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A
N E W S E T
O F
K

Logarithmic Solar Tables,

Calculated and constructed for determining the

LATITUDE at SEA,

BY TAKING

Two Altitudes of the Sun, with the intermediate Time, by a common Watch ; and that with Ease and Accuracy, independent of the Sun's meridional Altitude.

This most excellent and useful Performance, not only produces the true Latitude at any Time between Nine o'Clock in the Morning, and Three in the Afternoon ; but also gives the true Time of the Day, when the greatest Altitude was taken, to twenty Seconds ; and if greater Accuracy is required, proportional Parts may be taken. Whence the Sun's Azimuth may be determined by one single Proportion.

TO WHICH IS ADDED,

A COMPLETE THEORY,

Illustrating the RATIONALE of this most useful Discovery.

The SIXTH EDITION, with the TABLES enlarged.

L O N D O N:

Printed for J. MOUNT, T. PAGE, W. MOUNT, and
T. PAGE, on TOWER-HILL.

M,DCC,LXXXI.

The PROPRIETORS to the PUBLIC.

THESE Tables were offered to us by Mr. *Richard Harrison*, whose Name is subscribed to the Preface following, who assures us, in the strictest manner, that he obtained them in Manuscript from a *Hollander*, and that they have never been published : We therefore, being desirous to promote and encourage whatever has a Tendency to improve the Practice of Navigation, have purchased them of him, and hope they will prove acceptable to the Public, by answering the Purposes intended.



To the Honourable the

Admirals, Commodores, and Captains in the ROYAL NAVY,
and the Worthy Commanders of Ships in the MERCHANTS
SERVICE.

S I R S,

AS Trade and Navigation are the grand Source of Riches and Power, so is the Royal Navy the Protection of Commerce, and the Preservation (under Providence) of the Liberties, Rights, and Privileges of the *British* Nation, against the Attempts of its invidious Enemies: Every real Improvement therefore in Navigation, justly merits the Attention of the Public, particularly of those who are more immediately concerned in the same; that this useful Discovery will be found, by general Practice, to have a just Claim hereunto, and that in an eminent Degree, I am fully assured by my own Experience; I shall not therefore in this Preface make any further Comment upon its Utility, but only take Notice of a few Particulars antecedent, and then proceed to exhibit such plain, easy Instructions and Directions in the Application and Use, as that the same may (by once carefully reading over) become intelligible and familiar, even to such who are only acquainted with the common Rudiments of Navigation.

This late Improvement is in no wise confined to any particular Instrument for taking the Sun's Altitude, although the best for that Purpose are certainly to be preferred: I have also added a Table of Allowance for Heights above the Surface of the Water, and another of Refraction, which last, at some particular Times is more essentially to be considered and allowed, as hereafter I have noticed.

It is not intended that this should, or ought to destroy the usual Method of finding the Latitude by meridional Observations; it will certainly be right to take these as often as they can be taken, if it is only for the Satisfaction of comparing the Agreement; but it frequently happens

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happens that this cannot be obtained, by Reason of foggy Weather, a Squall, or the Interposition of a Cloud, especially when near the Land; and after a long Voyage, for Want of the true Latitude, it too often proves fatal; whereas if the true Latitude was known, a true Course could be shaped accordingly, (proper Allowances for Variation being made, and if Observations of the Variation cannot be had, there is an accurate Chart for that Purpose lately constructed by Mr. *William Mountaine*, F.R.S. and sold by Messrs. *Mounts and Pages*, on *Tower-Hill*) and a good Landfall made, or the great Dangers of a narrow Channel avoided.

This new Invention has had a thorough Inspection and Trial on Board some of his Majesty's Ships of War, and has been approved as the most exact and accurate Method that ever appeared for this Purpose, and by those to whom it was communicated for Trial, kept as a great Secret; yet notwithstanding this Secrecy, it has been delivered from one Friend to another for further Experiment, who greatly avail themselves of this Curiosity and Performance, and endeavour to distinguish themselves thereby, on which Account I think it ought not to be concealed any longer, but that the same deserves, and ought to be published for general Service.

I do then hereby declare, that although I have published this Matter, yet I am not the first Inventor of these Tables, but have so much Experience in regard to the practical Part and Improvements in them, that I can sufficiently testify the Truth thereof in real Practice.

The Determination of Longitude at Sea has been long attempted, but never yet rendered practicable, (that I know of) yet it is well known, that if such a Thing as an Automaton could be constructed, that would keep true equal Time (for which Mr. *Harrison* bids the fairest) it would be of great Utility in this Respect; yet then, this would not avail, unless the true Time of the Day could be had, but the true Time of the Day cannot always be obtained, even by a meridional Observation, for it is well known to those of Experience, that
the

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the apparent Velocity of the Sun, or the Alteration in his Altitude, (especially in Latitudes approaching his Zenith) is so small, that he appears almost stationary for some Time, whence the true Time of his passing the Meridian cannot be exactly or accurately adjusted by this Means.

And as a small Error in Time makes a considerable Error in Longitude, that is, as 15 Degrees of Longitude is to one Hour, or as one Minute of Time to 15 Miles of Longitude, it may happen to be of a very bad Consequence, if the true Time of Noon be not duly adjusted.

But if the true Time of the Day can be exactly found, then by such Machine the Longitude of the Place is precisely fixed: Hence arises the further very great Advantage of these Tables, as, besides the Latitude, they determine the exact and true Time of the Day when the greatest Altitude is taken, by pursuing the following Directions, and which I here recommend for the public Good and Safety of Navigation; which are the hearty Wishes of,

S I R S,

Your most obedient, and

Very humble Servant,

RICHARD HARRISON,

Of Whitehaven.

INSTRUCTIONS to the READER.

IT is to be observed in the first Place, that natural Sines are made Use of in the Performance of this Work ; and as every one has not Tables hereof, I shall shew the Practitioner how to find them by the common Tables of Logarithms and Artificial Sines, exact to four Places of Figures, which will answer the End for Computation of the Latitude to one Minute, or two, and regulating the Time to 20 Seconds ; but for greater Accuracy I would recommend *Sherwin's* Tables, which are exceedingly useful to the Astronomer and Navigator, and contain the Natural Sines, &c.

How to find the Natural Sines.

First, Enter the Tables of Artificial Sines, with the Degrees and Minutes given ; take those Figures answering thereto, only substituting 3, unless the Degree and Minute given be less than $5^{\circ} 45'$, when substitute 2 for the Index ; and therewith enter the Tables of Logarithms, and find the said Figures, or the nearest thereunto, the corresponding Number is the Natural Sine of the Degree and Minutes given : For further Illustration take an Example.

E X A M P L E.

Let it be required to find the Natural Sine of 54d. 7m.

The Artificial or Logarithmic Sine of 54d. 7m. is ——— 9.908599

Enter the Table of Logarithmic with the said Figures, only retaining 3 for the Index, and the nearest Log. is 3.908592, whose corresponding Number is 8102, the Natural Sine required exact to four Places.

Secondly, To find the Degrees and Minutes answering to any given Natural Sine.

This is done by reversing the former Rule.

E X A M P L E.

Let 8171 be the Natural Sine given, to find the corresponding Degrees and Minutes.

The Logarithm of 8171 you will find to be 3.912275; substitute 9 for the Index, instead of 3, and find the said Number, or the nearest thereto, in the Artificial Sines, which is 9.912299, whose corresponding Degrees and Minutes are 54d. 48m. If the Number of Places of Figures of the Natural Sines was only 2, the Index must be taken 8.

Thirdly, It may be necessary to explain what is meant by the Term *Arithmetical Complement*, an *Expression* used in the following Work.

Find the Artificial Sine of the Degrees and Minutes given, and subtract each Figure (beginning on the left Hand) from 9, except the last, which take from 10; the Remainder is the *Arithmetical Complement*, and is equivalent to subtracting the Whole from 10,000, &c.

E X A M P L E

What is the Arithmetical Complement of 46° 50'?

Enter the Table of Sines with 46° 50', gives 9.862946, each Figure taken from 9, &c. as above directed, leaves 0.137054, equivalent to 10.000000 less 9.862946.

Fourthly, To find the Logarithm Ratio.

It is to be observed, that in the following Operations, a supposed Latitude must be one of the Terms or Things given, in order to find the true Latitude and Time of the Day: This supposed Latitude must be your Latitude by Account when you take the Sun's Altitudes; but yet it does not require such an exact Computation, as to cast up the Log-board; an Estimation made by inspecting the Courses and Distances from last Noon will be sufficient, since an Error of 15 or 20 Minutes will in no wise affect the Latitude found by this new Invention, worthy of Notice; for if you designedly make an Error of one, two, or three Degrees, and repeat the Work two or three Times, still making use of the Latitude last found, for your supposed Latitude in the next Operation, it will at last discover itself to be the true, by being equal to the last

Sup-

Supposition, which evidently shews the Excellency of these *New Solar Tables*, preferable to any Methods heretofore made use of for these Purposes ; but to proceed to the Logarithm Ratio.

To the Arithmetical Complement of the Co-sine of the supposed Latitude, add the Arithmetical Complement of the Co-sine of the Declination, the Sum gives the Logarithm Ratio.

E X A M P L E.

The supposed Lat.	46° 50'	Co-sine	9.835134	Arith. Com.	{	0.16486
Sun's Declination	11° 17'	Co-sine	9.991523			0.00847
The Logarithm Ratio						0.17333

Or, which is the same Thing, and more facile ; to the Secant of the Latitude, add the Secant of the Declination, the Sum, abating twice Radius, will be the Logarithm Ratio, as above.

Fifthly, Due Regard must be had to the Times when the Sun's Altitudes were taken, and if both the Altitudes were taken in the Forenoon, they must be subtracted from each other, and half that Difference is called *half the Difference of elapsed Time* ; but if one Altitude be taken in the Forenoon, and the other in the Afternoon, to the Time in the Afternoon add 12h. and then subtract, gives the intermediate Time, as before ; and as in this last Case, some Difference of Longitude may be made between the Observations, you must allow one Minute of Time for every 15 Miles of Longitude, and subtract this Allowance from the Time elapsed between the Observations, if sailing to the Westward, but add, if sailing to the Eastward.

E X A M P L E S in each C A S E.

First, Both Altitudes in the Forenoon.

The First at _____	10h.	2m.
The second at _____	11h.	27m.
Subtract is the elapsed Time _____	1h.	25m.
Half the elapsed Time _____	0h.	42m. 30 sec.

Secondly, Sailing Westerly.

The first Altitude, Forenoon	—	10h. 26m.
The second Alt. Afternoon	—	14h. 43m.
Subtract	—	4h. 17m.
Diff. Lon. made is 30m. W. equal to	—	0h. 2m.
Subtract is the elapsed Time	—	4h. 15m.
Half the elapsed Time	—	2h. 7m. 30 sec.

Thirdly, Sailing Easterly.

The first Altitude, Forenoon	—	10h. 30m.
The second Alt. Afternoon	—	14h. 36m.
Subtract	—	4h. 6m.
Diff. Long. made is 15m. E. or equal to	—	0h. 1m.
Add, gives the elapsed Time	—	4h. 7m.
Half the elapsed Time	—	2h. 3m. 30 sec.

Lastly, The two Observations must be taken within three Hours of Noon, but the nearer to Noon the better, provided there is a proper Interval of Time between them, as follows. Both Observations in the Forenoon; the Interval must not be much less than half the Time of the first Observation from Noon. Both after Noon; the Interval must not be much less than the Time of the first Observation from Noon; one Observation before Noon, and the other after, the Interval must not exceed five Hours.

A TABLE shewing the Depression or Dip of the visible Horizon, below the true Horizontal Plane; according to several Heights (therein mentioned) of the Observer's Eye above the Surface of the Sea; to be subtracted from the Altitude found by the Instrument, and added to the Zenith Distance.

The Eye above the Surface
of the Sea in Feet.

Visible Horizon de-
press'd in Minutes.

1	1
3	2
7	3
12	3
18	4
27	5
35	6
40	6
45	6
50	7

A CORRECT Table of Refraction to be subtracted from the Altitude, or added to the Zenith Distance, found by the Instrument.

Deg. App. Alt.	Re- fraction.		Deg. App. Alt.	Re- fraction.		Deg. App. Alt.	Re- fraction.		Deg. App. Alt.	Re- fraction.	
deg.	m.	f.	deg.	m.	f.	deg.	m.	f.	deg.	m.	f.
0	33	0	12	4	23	29	1	42	46	0	55
$\frac{1}{2}$	28	22	13	4	3	30	1	38	47	0	53
1	24	29	14	3	45	31	1	35	48	0	51
$1\frac{1}{2}$	21	15	15	3	30	32	1	31	49	0	49
2	18	35	16	3	17	33	1	28	50	0	48
$2\frac{1}{2}$	16	24	17	3	4	34	1	24	51	0	46
3	14	36	18	2	54	35	1	21	52	0	44
$3\frac{1}{2}$	13	34	19	2	44	36	1	18	53	0	43
4	11	51	20	2	35	37	1	16	54	0	41
$4\frac{1}{2}$	10	48	21	2	27	38	1	13	55	0	40
5	9	54	22	2	20	39	1	10	60	0	33
6	8	28	23	2	14	40	1	8	65	0	26
7	7	20	24	2	7	41	1	5	70	0	21
8	6	29	25	2	2	42	1	3	75	0	15
9	5	48	26	1	56	43	1	1	80	0	10
10	5	15	27	1	51	44	0	59	85	0	5
11	4	47	28	1	47	45	0	57	90	0	0

The Application of the foregoing INSTRUCTIONS to Practice.

GENERAL RULE.

First, **T**O the Arithmetical Complement of the Co-sine of the Latitude by Account, add the Arithmetical Complement of the Co-sine of the Sun's Declination, that Sum is the Logarithm of the Ratio.

Secondly, Subtract the Hours and Minutes of Time when the Altitudes were taken from each other, and half the Remainder is called the *Half Difference of elapsed Time*.

Thirdly, Take the Natural Sine of each Altitude; subtract the less from the greater, that Difference call the *Remainder*.

Fourthly, Take the *Logarithm Ratio*, and the common Logarithm of the *Remainder*; also the Logarithm of *Half the elapsed Time* answerable to the Hours, Minutes, and Seconds in the following Tables; these three added into one Sum, give the *Logarithm of the middle Time*.

Fifthly, The Hours, Minutes and Seconds answering to this *Logarithm of Middle Time* being found in these Tables, subtract the same from the *half elapsed Time*, or *vice versa*, the half elapsed Time from the middle Time, the Remainder is the Time in Hours, Minutes, and Seconds, that the Sun had to ascend to the Meridian when the greatest Altitude was taken; then enter these Tables with this, under the Title of *Rising*, and from the Logarithm thereto corresponding, subtract the *Logarithm of the Ratio*, the Remainder is a common Logarithm, with which enter the common Table of Logarithms, and find the natural Number answering thereunto, due Regard being had to the Index.

Sixthly, To the Natural Sine of the Sun's greatest Altitude taken, add the Natural Number last found, their Sum is the Natural Sine of the Degree and Minute of the Sun's Meridional Altitude that Day, which are easily discovered by observing the second Rule in the former Directions concerning Natural Sines, if a Table of Natural Sines are not at Hand: And having obtained the Meridional Altitude, the Latitude is found by the usual Rules.

Lastly, Take the Hours, Minutes, and Seconds of the *Middle Time*, and also of *Half the elapsed Time*, subtract the less from the greater; this Dif-

ference is the true Time from Twelve o'Clock, or the Sun's passing over the Meridian, when the greatest Altitude was taken; compare this with the apparent Time by the Watch or Glass, and if they agree, your Watch goes true, if not, the Difference shews how much too fast or too slow.

N.B. These Tables are adapted to a Table of natural Sines where the Number of Places is 5 when greatest, the Radius being 100000. Therefore if a Table be used where the Number of Places is more, or the Radius greater than 100000, as many Figures must be left out to the right Hand as that Excess amounts to. Or in other Words; take the 5 first Places of Figures out of the Tables of Natural Sines, unless the Degree and Minute given be under $5^{\circ} 45'$ when take only 4 Places of Figures: And if the Sum found according to Precept 6th consists only of 4 Places of Figures, the Sun's Meridional Altitude is under $5^{\circ} 45'$.

For further Illustration, the following Examples are exhibited and performed at large.

E X A M P L E I.

AUGUST the 2d, 1772, Sun's Declination 11d. 17m. North, and at 10h. 2m. in the Forenoon, the Sun's Altitude was 46d. 55m. then again at 11h. 27m. the second Altitude was 54d. 7m. Latitude by Account is 46d. 50m. North, required the true Latitude and true Time of the Day, when the greatest Altitude was taken?

h. m. f.

At—11	27	0	Lat. by Account, Arith. Comp. of its Co-sine—	0.16486
At—10	2	0	Sun's Declination, Arith. Comp. of its Co-sine—	0.00847
Elap.	1	25	0 Added, gives the Logarithm Ratio—	0.17333
	0	42	30 Half the elapsed Time	

The Sun's greatest Alt. at 11h. 27m. is 54d. 7m. Natural Sine — 81020

The Sun's Alt. taken at 10h. 2m. is 46d. 55m. Natural Sine — 73030

Subtract ————— the Remainder 7990

The Logarithm Ratio ————— 0.17333

Common Logarithm of the Remainder ————— 3.90255

Logarithm of half elapsed Time 42m. 30 sec. ————— 0.73429

The Sum is the Logarithm of middle Time ————— 4.81017

h. m. s.

The Hour and Min. &c. for which by these Tables is ——— 1 15 30
 Subtract from it half elapsed Time ——— 0 42 30
 Their Diff. is the true Space of Time the Sun had to rise to the }
 Meridian, when the great Altitude was taken ——— 0 33 0
 By the Watch at — 11h. 27m. }
 Subtract it from — 12h. 0m. } So I find they agree, and the Watch
 Remains ——— 0h. 33m. } must be exactly right.

Log. of Rising

Lastly, Enter these Tables with 33m. under Rising ——— 3.01488
 Ratio subtract from it ——— 0.17333
 Remains a common Logarithm, whose Natural Number must }
 be found ——— 2.84155
 To the Natural Sine of the greatest Altitude ——— 81020
 Add the Natural Number of the above Logarithm ——— 694
 Sum is the Natural Sine of the Sun's Meridian Altitude ——— 81714

d. m.

The Degrees, &c. corresponding are 54 48
 Subtract from ——— 90 0
 The Sun's Zenith Distance ——— 35 12 S } That Day at Noon it was
 Sun's Declination add ——— 11 17 N } by Observation found to
 Latitude at Noon ——— 46 29 N } be 46d. 30m. North.

EXAMPLE II.

The Sun's Declination and Latitude as before, but at 10h. 26m. in the Forenoon, the First Altitude was 49d. 13m. the second Altitude in the Afternoon 41d. 13m. at 43 Minutes past two, at this Time had made 30m. Difference of Longitude, sailing to the Westward, I demand the Latitude when the greatest Altitude was taken, and Hour of Day?

Supposed Lat. 46d. 50m. N. Arithmetical Comp. of its Co-sine 0.16486
 Sun's Decl. 11d. 17m. N. Arithmetical Comp. of its Co-sine 0.00847
 The Logarithm Ratio ——— 0.17333
 Forenoon Altitude 49d. 13m. its Natural Sine ——— 75720
 Afternoon Altitude 41d. 13m. its Natural Sine ——— 65890
 The Remainder ——— 9830

D

h. m. s.

	h. m. f.		
Afternoon	14 43 0	Logarithm Ratio	0.17333
Forenoon	10 26 0	Common Logarithm Remainder	3.99255
		Logarithm of half elapsed Time	0.27731
	4 17 0		
For 30 Miles	} 0 2 0	Logarithm of Middle Time	4.44319
Diff. Longit		Equal to oh. 32m. of. as by these Tables	
	4 15 0		
$\frac{1}{2}$ elapsed Time	2 7 30		
Subtract	0 32 0		
Remains	1 35 30	The Sun's Diff. when greatest Al. was taken	
Time by the	} 1 34 0	Logarithm of 1h. 35m. 30f. called	} 3.93232
Watch from 12 Hours.		Rising	
Remains	0 1 30	Ratio from it subtract	0.17333
Watch too fast	1 $\frac{1}{2}$ m.	A common Logarithm	3.75899
Whose Natural Number is 5741—add to greatest Alt. Natural Sine 75720			

5741

Their Sum is the Natural Sine of the Sun's Meri. Alt. $54^{\circ} 33'$ — 81461

Or the Artificial Sine of 81461 gives — 54d. 33m.

From ————— 90d. 0m.

Sun's Zenith Distance ————— 35d. 27 S.

Sun's Declination ————— 11d. 17 N.

Latitude at Noon ————— 46d. 44 N.

EXAMPLE III.

Sailing to the Eastward, the Sun's Declination 3d. 38m. N. the first Altitude Forenoon 46d. 2m. the second Altitude Afternoon 35d. 43m. Difference of Longitude made is 15 Miles E. the greater Altitude at 10h. 30m. the less at 36m. past two in the Afternoon; Latitude by Account 43d. 30m. required the true Time of the Day, and Latitude of the Place at the greatest Altitude.

Lat.

Lat. by Account—43d. 30m. N. Arith. Comp. of its Co-sine 0.13943
 Sun's Declination— 3d. 38m. N. Arith. Comp. of its Co-sine 0.00087
 The Logarithm Ratio ————— 0.14030

Forenoon Altitude 46d. 2m. Natural Sine ————— 71970
 Afternoon Altitude 35d. 43m. Natural Sine ————— 58370
 The Remainder ————— 13600

	h.	m.	f.		
Afternoon ———	14	36	0	Logarithm Ratio ———	0.14030
Forenoon ———	10	30	0	Common Logarithm Remainder	4.13353
	4	6	0	Half elapsed Time ———	0.28974
Diff. Longit. 15 } Miles add 1 min. }	0	1	0	Logarithm of Middle Time ———	4.56357
	4	7	0	Equal to ——— oh. 42m. of:	
$\frac{1}{2}$ elapsed Time ———	2	3	30	Logarithm of 1h. 21m. 30f. rising	3.79634
Subtract ———	0	42	0	Ratio from it. ———	0.14030
True Time ———	1	21	30	Common Logarithm ———	3.65604
Sun had to rise by } the Watch }	1	30	0		
Difference ———	0	8	30		
Watch too slow $8\frac{1}{2}$ Minutes.					

The Natural Sine of the greatest Altitude ————— 71970
 The Natural Number of the Common Logarithm 3.65604 is — 4529
 Their Sum ————— 76499

The Artificial Sine of 76499, or Natural Sine 7650 —49d. 54m.
 From ————— 90d. 0m.
 Sun's Zenith Distance ————— 4d. 6m. S.
 Sun's Declination add ————— 3d. 38m. N.
 Latitude at Noon ————— 43d. 44m. N.

Having thus found the true Latitude to be 43d. 44m. and the Time by the Watch corrected 10h. 38m. 30f. when the Sun's Morning Altitude was taken, we may find the true Time from Noon thus :

Comp.

	d. m.		
Comp. Lat. —————	46 16	Comp. Lat. Co. Ar. ————	0.141123
Comp. Alt. —————	43 58	Comp. Dec. Co. Ar. ————	0.000874
Comp. Declin. ————	86 22	Sine of half Sum ————	0.999809
Sum	176 36	Sine of the Remainder ———	9.844372
$\frac{1}{2}$ Sum from which } ———	88 18	Sum	19.986178
sub. Co. Alt. ————		Half Sum	9.993089
Remainder —————	44 20		
		d. m.	
Equal to —————		79 48	
Doubled —————		159 36	
Subtract from ———		180 00	
Remains —————		20 24	

Equal to 1h. 21m. 36f. from Noon nearly.

The Time from Noon by the Work in the last Example appears to be 1h. 21m. 30f. differing only six Seconds.

By help of these Operations the true Azimuth is easily determined, having opposite Sides and Angles given; and as a tolerable Watch cannot be supposed to vary in the Space of one, two or three Hours, the same being duly rectified and adjusted, as before laid down, the Azimuth may be taken at any reasonable Time afterwards, and the Variation of the Compass ascertained in a very easy and familiar Manner, as in the following

E X A M P L E.

In the Latitude of 51d. 30m. North, the Sun's Declination 15d. 10m. North, at two Minutes past six in the Afternoon, the Sun's Altitude was 11d. 30m. the Sun's true Azimuth is required at that Time?

The P R O P O R T I O N.

As the Co-sine of the Sun's Altitude ————— 78d. 30m. — 9.991193
 Is to the Sine of the Hour from Noon — 6h. 2m. — 90 30 — 9.999983
 So is the Co-sine of the Sun's Declination ————— 74 50 — 9.084603
19.984586
 To the Sine of the Sun's Azimuth ————— = 80 2 — 9.993393
 Or its Supplement to 180° from the elevated Pole.

The

The New LOGARITHMIC SOLAR TABLES. 17

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
0	0	20	2.83730	2.46373	1.02436	0	12	20	1.26931	4.03172	2.16066
0	0	30	2.66121	2.63982	1.37654	0	12	30	1.26349	4.03754	2.17223
0	0	40	2.53627	2.76476	1.62642	0	12	40	1.25774	4.04329	2.18382
0	1	00	2.36018	2.94085	1.97860	0	13	00	1.24647	4.05456	2.20638
0	1	20	2.23525	3.06578	0.22848	0	13	20	1.23549	4.06554	2.22836
0	1	30	2.18409	3.11694	0.33079	0	13	30	1.23010	4.07093	2.23915
0	1	40	2.13834	3.16269	0.42230	0	13	40	1.22477	4.07626	2.24980
0	2	00	2.05916	3.24187	0.58066	0	14	00	1.21432	4.08671	2.27073
0	2	20	1.99221	3.30883	0.71455	0	14	20	1.20412	4.09691	2.29116
0	2	30	1.96225	3.33878	0.77448	0	14	30	1.19910	4.10193	2.30120
0	2	40	1.93422	3.36681	0.83054	0	14	40	1.19415	4.10688	2.31112
0	3	00	1.88307	3.41796	0.93284	0	15	00	1.18440	4.11663	2.33063
0	3	20	1.83732	3.46371	1.02435	0	15	20	1.17487	4.12616	2.34972
0	3	30	1.81613	3.48490	1.06673	0	15	30	1.17018	4.13085	2.35910
0	3	40	1.79593	3.50510	1.10714	0	15	40	1.16554	4.13549	2.36839
0	4	00	1.75814	3.54289	1.18271	0	16	00	1.15642	4.14461	2.38667
0	4	20	1.72339	3.57764	1.25224	0	16	20	1.14748	4.15355	2.40457
0	4	30	1.70700	3.59403	1.28502	0	16	30	1.14307	4.15796	2.41338
0	4	40	1.69121	3.60982	1.31660	0	16	40	1.13872	4.16231	2.42211
0	5	00	1.66125	3.63978	1.37653	0	17	00	1.13013	4.17090	2.43930
0	5	20	1.63322	3.66781	1.43258	0	17	20	1.12171	4.17932	2.45616
0	5	30	1.61986	3.68117	1.45931	0	17	30	1.11757	4.18346	2.46447
0	5	40	1.60690	3.69413	1.48524	0	17	40	1.11346	4.18757	2.47270
0	6	00	1.58208	3.71895	1.53488	0	18	00	1.10536	4.19567	2.48893
0	6	20	1.55861	3.74242	1.58184	0	18	20	1.09740	4.20363	2.50486
0	6	30	1.54733	3.75370	1.60440	0	18	30	1.09348	4.20755	2.51271
0	6	40	1.53634	3.76469	1.62639	0	18	40	1.08960	4.21143	2.52050
0	7	00	1.51515	3.78588	1.66877	0	19	00	1.08193	4.21910	2.53586
0	7	20	1.49496	3.80607	1.70917	0	19	20	1.07439	4.22664	2.55096
0	7	30	1.48520	3.81583	1.72869	0	19	30	1.07067	4.23036	2.55841
0	7	40	1.47566	3.82537	1.74778	0	19	40	1.06698	4.23405	2.56580
0	8	00	1.45718	3.84385	1.78474	0	20	00	1.05970	4.24133	2.58039
0	8	20	1.43946	3.86157	1.82019	0	20	20	1.05254	4.24849	2.59473
0	8	30	1.43086	3.87017	1.83739	0	20	30	1.04901	4.25202	2.60182
0	8	40	1.42243	3.87860	1.85426	0	20	40	1.04550	4.25553	2.60885
0	9	00	1.40605	3.89498	1.88703	0	21	00	1.03857	4.26246	2.62274
0	9	20	1.39027	3.91076	1.91862	0	21	20	1.03175	4.26928	2.63641
0	9	30	1.38258	3.91845	1.93399	0	21	30	1.02838	4.27265	2.64316
0	9	40	1.37503	3.92600	1.94909	0	21	40	1.02504	4.27599	2.64987
0	10	00	1.36032	3.94071	1.97854	0	22	00	1.01843	4.28260	2.66312
0	10	20	1.34609	3.95494	2.00699	0	22	20	1.01192	4.28911	2.67617
0	10	30	1.33915	3.96188	2.02091	0	22	30	1.00870	4.29233	2.68262
0	10	40	1.33231	3.96872	2.03458	0	22	40	1.00550	4.29553	2.68903
0	11	00	1.31896	3.98207	2.06131	0	23	00	0.99918	4.30185	2.70169
0	11	20	1.30600	3.99503	2.08723	0	23	20	0.99296	4.30807	2.71418
0	11	30	1.29967	4.00136	2.09991	0	23	30	0.98988	4.31115	2.72036
0	11	40	1.29342	4.00761	2.11240	0	23	40	0.98682	4.31421	2.72649
0	12	00	1.28120	4.01983	2.13867	0	24	00	0.98077	4.32026	2.73863

18 The New LOGARITHMIC SOLAR TABLES.

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
0	24	20	0.97480	4.32623	2.75060	0	36	20	0.80170	4.49933	3.09830
0	24	30	0.97184	4.32919	2.75652	0	36	30	0.79973	4.50130	3.10227
0	24	40	0.96891	4.33212	2.76241	0	36	40	0.79777	4.50326	3.10622
0	25	00	0.96310	4.33793	2.77405	0	37	00	0.79387	4.50716	3.11406
0	25	20	0.95738	4.34365	2.78555	0	37	20	0.79001	4.51102	3.12184
0	25	30	0.95454	4.34649	2.79124	0	37	30	0.78809	4.51294	3.12570
0	25	40	0.95172	4.34931	2.79689	0	37	40	0.78618	4.51485	3.12954
0	26	00	0.94614	4.35489	2.80809	0	38	00	0.78239	4.51864	3.13718
0	26	20	0.94063	4.36040	2.81914	0	38	20	0.77863	4.52240	3.14175
0	26	30	0.93790	4.36313	2.82461	0	38	30	0.77677	4.52426	3.14850
0	26	40	0.93519	4.36584	2.83005	0	38	40	0.77491	4.52612	3.15225
0	27	00	0.92982	4.37121	2.84083	0	39	00	0.77122	4.52981	3.15969
0	27	20	0.92452	4.37651	2.85148	0	39	20	0.76756	4.53347	3.16706
0	27	30	0.92189	4.37914	2.85675	0	39	30	0.76574	4.53529	3.17072
0	27	40	0.91928	4.38175	2.86199	0	39	40	0.76393	4.53710	3.17437
0	28	00	0.91411	4.38692	2.87238	0	40	00	0.76033	4.54070	3.18162
0	28	20	0.90899	4.39204	2.88265	0	40	20	0.75676	4.54427	3.18881
0	28	30	0.90646	4.39457	2.88773	0	40	30	0.75499	4.54604	3.19238
0	28	40	0.90394	4.39709	2.89279	0	40	40	0.75323	4.54780	3.19594
0	29	00	0.89894	4.40209	2.90282	0	41	00	0.74972	4.55131	3.20301
0	29	20	0.89401	4.40702	2.91273	0	41	20	0.74624	4.55479	3.21003
0	29	30	0.89156	4.40947	2.91765	0	41	30	0.74451	4.55652	3.21351
0	29	40	0.88913	4.41190	2.92254	0	41	40	0.74279	4.55824	3.21698
0	30	00	0.88430	4.41673	2.93223	0	42	00	0.73937	4.56166	3.22389
0	30	20	0.87953	4.42150	2.94181	0	42	20	0.73597	4.56506	3.23073
0	30	30	0.87717	4.42386	2.94656	0	42	30	0.73429	4.56674	3.23414
0	30	40	0.87481	4.42622	2.95129	0	42	40	0.73261	4.56842	3.23753
0	31	00	0.87015	4.43088	2.96067	0	43	00	0.72926	4.57177	3.24427
0	31	20	0.86553	4.43550	2.96994	0	43	20	0.72595	4.57508	3.25095
0	31	30	0.86324	4.43779	2.97454	0	43	30	0.72430	4.57673	3.25428
0	31	40	0.86096	4.44007	2.97912	0	43	40	0.72266	4.57837	3.25759
0	32	00	0.85644	4.44459	2.98820	0	44	00	0.71940	4.58163	3.26418
0	32	20	0.85197	4.44906	2.99718	0	44	20	0.71616	4.58487	3.27072
0	32	30	0.84976	4.45127	2.00164	0	44	30	0.71455	4.58648	3.27396
0	32	40	0.84755	4.45348	2.00608	0	44	40	0.71295	4.58108	3.27720
0	33	00	0.84317	4.45786	2.01488	0	45	00	0.70976	4.59127	3.28363
0	33	20	0.83884	4.46219	2.02360	0	45	20	0.70660	4.59443	3.29002
0	33	30	0.83669	4.46434	2.02792	0	45	30	0.70503	4.59600	3.29320
0	33	40	0.83455	4.46648	2.03222	0	45	40	0.70346	4.59751	3.29637
0	34	00	0.83030	4.47073	2.04077	0	46	00	0.70034	4.60069	3.30266
0	34	20	0.82609	4.47494	2.04922	0	46	20	0.69725	4.60378	3.30891
0	34	30	0.82401	4.47702	2.05342	0	46	30	0.69571	4.60532	3.31202
0	34	40	0.82193	4.47910	2.05760	0	46	40	0.69418	4.60685	3.31512
0	35	00	0.81780	4.48323	2.06590	0	47	00	0.69113	4.60990	3.32128
0	35	20	0.81372	4.48731	2.07411	0	47	20	0.68811	4.61292	3.32739
0	35	30	0.81169	4.48934	2.07819	0	47	30	0.68660	4.61443	3.33044
0	35	40	0.80967	4.49136	2.08225	0	47	40	0.68510	4.61593	3.33347
0	36	00	0.80567	4.49536	2.09032	0	48	00	0.68212	4.61892	3.33950

The New LOGARITHMIC SOLAR TABLES. 19

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
0	48	20	0.67916	4.62187	3.34549	1	60	20	0.58465	4.71638	3.53721
0	48	30	0.67769	4.52334	3.34847	1	60	30	0.58348	4.71755	3.53959
0	48	40	0.67622	4.62481	3.35144	1	60	40	0.58231	4.71872	3.54197
0	49	00	0.67330	4.62773	3.35734	1	1	00	0.57999	4.72104	3.54670
0	49	20	0.67040	4.63063	3.36321	1	1	20	0.57768	4.72335	3.55140
0	49	30	0.66896	4.63207	3.36613	1	1	30	0.57653	4.72450	3.55375
0	49	40	0.66752	4.63351	3.36903	1	1	40	0.57538	4.72565	3.55608
0	50	00	0.66466	4.63637	3.37482	1	2	00	0.57310	4.72793	3.56074
0	50	20	0.66182	4.63921	3.38057	1	2	20	0.57083	4.73020	3.56537
0	50	30	0.66041	4.64062	3.38343	1	2	30	0.56970	4.73133	3.56767
0	50	40	0.65900	4.64203	3.38628	1	2	40	0.56857	4.73246	3.56997
0	51	00	0.65620	4.64483	3.39195	1	3	00	0.56633	4.73470	3.57455
0	51	20	0.65342	4.64761	3.39759	1	3	20	0.56409	4.73694	3.57910
0	51	30	0.65204	4.64899	3.40039	1	3	30	0.56298	4.73805	3.58137
0	51	40	0.65066	4.65037	3.40318	1	3	40	0.56187	4.73916	3.58363
0	52	00	0.64791	4.65312	3.40875	1	4	00	0.55966	4.74137	3.58814
0	52	20	0.64519	4.65584	3.41427	1	4	20	0.55746	4.74357	3.59262
0	52	30	0.64383	4.65720	3.41702	1	4	30	0.55637	4.74466	3.59486
0	52	40	0.64248	4.65855	3.41976	1	4	40	0.55528	4.74575	3.59708
0	53	00	0.63978	4.66125	3.42523	1	5	00	0.55311	4.74792	3.60152
0	53	20	0.63711	4.66392	3.43064	1	5	20	0.55095	4.75008	3.60593
0	53	30	0.63578	4.66525	3.43334	1	5	30	0.54987	4.75116	3.60813
0	53	40	0.63445	4.66658	3.43603	1	5	40	0.54880	4.75223	3.61032
0	54	00	0.63181	4.66922	3.44138	1	6	00	0.54666	4.75437	3.61469
0	54	20	0.62919	4.67184	3.44670	1	6	20	0.54453	4.75650	3.61903
0	54	30	0.62789	4.67314	3.44935	1	6	30	0.54347	4.75756	3.62120
0	54	40	0.62659	4.67444	3.45199	1	6	40	0.54241	4.75862	3.62336
0	55	00	0.62400	4.67703	3.45724	1	7	00	0.54031	4.76072	3.62766
0	55	20	0.62142	4.67961	3.46247	1	7	20	0.53822	4.76281	3.63194
0	55	30	0.62014	4.68089	3.46507	1	7	30	0.53718	4.76385	3.63407
0	55	40	0.61886	4.68217	3.46765	1	7	40	0.53614	4.76489	3.63620
0	56	00	0.61632	4.68471	3.47282	1	8	00	0.53406	4.76697	3.64043
0	56	20	0.61380	4.68723	3.47795	1	8	20	0.53200	4.76903	3.64465
0	56	30	0.61254	4.68849	3.48050	1	8	30	0.53097	4.77006	3.64675
0	56	40	0.61129	4.68974	3.48305	1	8	40	0.52995	4.77108	3.64885
0	57	00	0.60879	4.69224	3.48811	1	9	00	0.52791	4.77312	3.65302
0	57	20	0.60631	4.69472	3.49315	1	9	20	0.52589	4.77514	3.65717
0	57	30	0.60508	4.69595	3.49566	1	9	30	0.52488	4.77615	3.65924
0	57	40	0.60385	4.69718	3.49816	1	9	40	0.52387	4.77716	3.66131
0	58	00	0.60140	4.69963	3.50314	1	10	00	0.52186	4.77917	3.66542
0	58	20	0.59896	4.70207	3.50809	1	10	20	0.51986	4.78117	3.66952
0	58	30	0.59775	4.70328	3.51056	1	10	30	0.51886	4.78217	3.67156
0	58	40	0.59654	4.70449	3.51301	1	10	40	0.51787	4.78316	3.67359
0	59	00	0.59414	4.70689	3.51791	1	11	00	0.51589	4.78514	3.67756
0	59	20	0.59173	4.70928	3.52278	1	11	20	0.51392	4.78711	3.68168
0	59	30	0.59056	4.71047	3.52520	1	11	30	0.51294	4.78809	3.68369
0	59	40	0.58937	4.71166	3.52761	1	11	40	0.51196	4.78907	3.68570
1	60	00	0.58700	4.71403	3.53243	1	12	00	0.51002	4.79101	3.68969

20 The New LOGARITHMIC SOLAR TABLES.

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
1	12	20	0.50808	4.79295	3.69367	1	24	20	0.44403	4.85700	3.82570
1	12	30	0.50711	4.79392	3.69566	1	24	30	0.44321	4.85782	3.82739
1	12	40	0.50615	4.79488	3.69763	1	24	40	0.44239	4.85864	3.82908
1	13	00	0.50423	4.79680	3.70158	1	25	00	0.44077	4.86026	3.83246
1	13	20	0.50232	4.79871	3.70550	1	25	20	0.43915	4.86188	3.83582
1	13	30	0.50137	4.79966	3.70745	1	25	30	0.43834	4.86269	3.83749
1	13	40	0.50042	4.80061	3.70940	1	25	40	0.43753	4.86350	3.83917
1	14	00	0.49852	4.80251	3.71329	1	26	00	0.43593	4.86510	3.84250
1	14	20	0.49664	4.80439	3.71716	1	26	20	0.43433	4.86670	3.84582
1	14	30	0.49570	4.80533	3.71909	1	26	30	0.43353	4.86750	3.84748
1	14	40	0.49476	4.80627	3.72101	1	26	40	0.43273	4.86830	3.84913
1	15	00	0.49200	4.80813	3.72485	1	27	00	0.43114	4.86989	3.85242
1	15	20	0.49104	4.80999	3.72867	1	27	20	0.42956	4.87147	3.85570
1	15	30	0.49012	4.81091	3.73057	1	27	30	0.42877	4.87226	3.85734
1	15	40	0.48920	4.81183	3.73247	1	27	40	0.42799	4.87304	3.85897
1	16	00	0.48736	4.81367	3.73625	1	28	00	0.42643	4.87460	3.86223
1	16	20	0.48553	4.81550	3.74001	1	28	20	0.42487	4.87616	3.86547
1	16	30	0.48462	4.81641	3.74189	1	28	30	0.42409	4.87694	3.86709
1	16	40	0.48371	4.81732	3.74376	1	28	40	0.42331	4.87772	3.86870
1	17	00	0.48189	4.81914	3.74750	1	29	00	0.42176	4.87927	3.87192
1	17	20	0.48009	4.82004	3.75121	1	29	20	0.42022	4.88081	3.87513
1	17	30	0.47919	4.82184	3.75307	1	29	30	0.41945	4.88158	3.87672
1	17	40	0.47829	4.82274	3.75491	1	29	40	0.41868	4.88235	3.87832
1	18	00	0.47650	4.82453	3.75860	1	30	00	0.41716	4.88387	3.88150
1	18	20	0.47472	4.82631	3.76227	1	30	20	0.41564	4.88539	3.88467
1	18	30	0.47383	4.82720	3.76409	1	30	30	0.41488	4.88615	3.88625
1	18	40	0.47295	4.82808	3.76592	1	30	40	0.41412	4.88691	3.88783
1	19	00	0.47119	4.82984	3.76955	1	31	00	0.41261	4.88842	3.89097
1	19	20	0.46943	4.83160	3.77318	1	31	20	0.41111	4.88992	3.89411
1	19	30	0.46856	4.83247	3.77498	1	31	30	0.41036	4.89067	3.89567
1	19	40	0.46769	4.83334	3.77678	1	31	40	0.40961	4.89142	3.89723
1	20	00	0.46595	4.83508	3.78037	1	32	00	0.40812	4.89291	3.90034
1	20	20	0.46421	4.83682	3.78395	1	32	20	0.40664	4.89439	3.90344
1	20	30	0.46335	4.83768	3.78573	1	32	30	0.40590	4.89513	3.90498
1	20	40	0.46249	4.83854	3.78759	1	32	40	0.40516	4.89587	3.90653
1	21	00	0.46077	4.84026	3.79195	1	33	00	0.40368	4.89735	3.90960
1	21	20	0.45907	4.84196	3.79458	1	33	20	0.40222	4.89881	3.91267
1	21	30	0.45822	4.84281	3.79634	1	33	30	0.40149	4.89954	3.91420
1	21	40	0.45737	4.84366	3.79809	1	33	40	0.40076	4.90027	3.91572
1	22	00	0.45567	4.84536	3.80159	1	34	00	0.39930	4.90173	3.91876
1	22	20	0.45399	4.84704	3.80508	1	34	20	0.39785	4.90318	3.92179
1	22	30	0.45315	4.84788	3.80682	1	34	30	0.39713	4.90390	3.92331
1	22	40	0.45231	4.84872	3.80855	1	34	40	0.39641	4.90462	3.92482
1	23	00	0.45064	4.85039	3.81201	1	35	00	0.39497	4.90606	3.92782
1	23	20	0.44898	4.85205	3.81545	1	35	20	0.39353	4.90750	3.93082
1	23	30	0.44815	4.85288	3.81717	1	35	30	0.39282	4.90821	3.93232
1	23	40	0.44732	4.85371	3.81888	1	35	40	0.39211	4.90892	3.93381
1	24	00	0.44567	4.85536	3.82230	1	36	00	0.39069	4.91034	3.93679

The New LOGARITHMIC SOLAR TABLES. 21

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
I	36	20	0.38927	4.91176	3.93975	I	48	20	0.34172	4.95931	4.04003
I	36	30	0.38856	4.91247	3.94123	I	48	30	0.34110	4.95993	4.04134
I	36	40	0.38786	4.91317	3.94271	I	48	40	0.34048	4.96055	4.04265
I	37	00	0.38646	4.91457	3.94466	I	49	00	0.33925	4.96178	4.04526
I	37	20	0.38506	4.91597	3.95859	I	49	20	0.33803	4.96300	4.04786
I	37	30	0.38436	4.91667	3.95005	I	49	30	0.33742	4.96361	4.04916
I	37	40	0.38366	4.91737	3.95151	I	49	40	0.33681	4.96422	4.05045
I	38	00	0.38227	4.91876	3.95443	I	50	00	0.33559	4.96544	4.05304
I	38	20	0.38089	4.92014	3.95733	I	50	20	0.33438	4.96665	4.05561
I	38	30	0.38020	4.92083	3.95878	I	50	30	0.33378	4.96725	4.05690
I	38	40	0.37951	4.92152	3.96023	I	50	40	0.33318	4.96785	4.05818
I	39	00	0.37813	4.92290	3.96311	I	51	00	0.33197	4.96906	4.06074
I	39	20	0.37677	4.92426	3.96599	I	51	20	0.33077	4.97026	4.06330
I	39	30	0.37609	4.92494	3.96742	I	51	30	0.33017	4.97086	4.06457
I	39	40	0.37541	4.92562	3.96885	I	51	40	0.32958	4.97145	4.06584
I	40	00	0.37405	4.92698	3.97170	I	52	00	0.32839	4.97264	4.06838
I	40	20	0.37269	4.92834	3.97455	I	52	20	0.32720	4.97383	4.07091
I	40	30	0.37202	4.92901	3.97597	I	52	30	0.32661	4.97442	4.07217
I	40	40	0.37135	4.92968	3.97738	I	52	40	0.32602	4.97501	4.07343
I	41	00	0.37001	4.93102	3.97021	I	53	00	0.32485	4.97618	4.07595
I	41	20	0.36867	4.93236	3.98302	I	53	20	0.32367	4.97736	4.07845
I	41	30	0.36800	4.93303	3.98443	I	53	30	0.32309	4.97794	4.07970
I	41	40	0.36734	4.93369	3.98583	I	53	40	0.32250	4.97853	4.08095
I	42	00	0.36602	4.93501	3.98862	I	54	00	0.32134	4.97969	4.08344
I	42	20	0.36470	4.93633	3.99141	I	54	20	0.32018	4.98085	4.08592
I	42	30	0.36404	4.93699	3.99280	I	54	30	0.31960	4.98143	4.08716
I	42	40	0.36338	4.93765	3.99419	I	54	40	0.31902	4.98201	4.08840
I	43	00	0.36206	4.93897	3.99696	I	55	00	0.31787	4.98316	4.09087
I	43	20	0.36070	4.94027	3.99972	I	55	20	0.31672	4.98431	4.09333
I	43	30	0.36011	4.94092	4.00109	I	55	30	0.31614	4.98489	4.09456
I	43	40	0.35946	4.94157	4.00247	I	55	40	0.31557	4.98546	4.09578
I	44	00	0.35816	4.94287	4.00521	I	56	00	0.31443	4.98660	4.09823
I	44	20	0.35686	4.94417	4.00793	I	56	20	0.31329	4.98774	4.10067
I	44	30	0.35622	4.94481	4.00930	I	56	30	0.31272	4.98831	4.10188
I	44	40	0.35558	4.94545	4.01006	I	56	40	0.31216	4.98887	4.10310
I	45	00	0.35430	4.94673	4.01337	I	57	00	0.31103	4.99000	4.10552
I	45	20	0.35302	4.94801	4.01608	I	57	20	0.30990	4.99113	4.10794
I	45	30	0.35238	4.94865	4.01743	I	57	30	0.30934	4.99169	4.10915
I	45	40	0.35174	4.94929	4.01877	I	57	40	0.30878	4.99225	4.11035
I	46	00	0.35047	4.95056	4.02146	I	58	00	0.30776	4.99337	4.11275
I	46	20	0.34921	4.95182	4.02414	I	58	20	0.30655	4.99448	4.11515
I	46	30	0.34858	4.95245	4.02547	I	58	30	0.30599	4.99504	4.11634
I	46	40	0.34795	4.95308	4.02681	I	58	40	0.30544	4.99559	4.11754
I	47	00	0.34669	4.95434	4.02947	I	59	00	0.30433	4.99670	4.11992
I	47	20	0.34544	4.95559	4.03212	I	59	20	0.30323	4.99780	4.12229
I	47	30	0.34482	4.95621	4.03344	I	59	30	0.30268	4.99835	4.12348
I	47	40	0.34420	4.95683	4.03477	I	59	40	0.30213	4.99890	4.12466
I	48	00	0.34296	4.95807	4.03740	2	00	00	0.30103	5.00000	4.12702

22 The New LOGARITHMIC SOLAR TABLES.

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
2	00	20	0.29994	5.00109	4.12938	2	12	20	0.26292	5.03811	4.20984
2	00	30	0.29939	5.00164	4.13055	2	12	30	0.26244	5.03859	4.21091
2	00	40	0.29885	5.00218	4.13172	2	12	40	0.26195	5.03908	4.21197
2	01	00	0.29776	5.00327	4.13406	2	13	00	0.26099	5.04004	4.21409
2	1	20	0.29668	5.00435	4.13640	2	13	20	0.26003	5.04100	4.21620
2	1	30	0.29614	5.00481	4.13756	2	13	30	0.25955	5.04148	4.21725
2	1	40	0.29560	5.00543	4.13872	2	13	40	0.25907	5.04196	4.21831
2	2	00	0.29453	5.00650	4.14104	2	14	00	0.25811	5.04292	4.22041
2	2	20	0.29346	5.00757	4.14336	2	14	20	0.25716	5.04387	4.22250
2	2	30	0.29293	5.00810	4.14451	2	14	30	0.25668	5.04435	4.22355
2	2	40	0.29239	5.00864	4.14566	2	14	40	0.25621	5.04482	4.22459
2	3	00	0.29133	5.00970	4.14797	2	15	00	0.25526	5.04577	4.22668
2	3	20	0.29027	5.01076	4.15026	2	15	20	0.25432	5.04671	4.22876
2	3	30	0.28974	5.01129	4.15140	2	15	30	0.25385	5.04718	4.22980
2	3	40	0.28921	5.01182	4.15255	2	15	40	0.25338	5.04765	4.23083
2	4	00	0.28816	5.01287	4.15483	2	16	00	0.25244	5.04859	4.23290
2	4	20	0.28711	5.01392	4.15710	2	16	20	0.25150	5.04953	4.23495
2	4	30	0.28659	5.01444	4.15824	2	16	30	0.25104	5.04999	4.23599
2	4	40	0.28607	5.01496	4.15937	2	16	40	0.25057	5.05046	4.23702
2	5	00	0.28502	5.01601	4.16163	2	17	00	0.24964	5.05139	4.23907
2	5	20	0.28398	5.01705	4.16389	2	17	20	0.24872	5.05231	4.24112
2	5	30	0.28346	5.01757	4.16501	2	17	30	0.24825	5.05278	4.24214
2	5	40	0.28295	5.01808	4.16614	2	17	40	0.24779	5.05324	4.24316
2	6	00	0.28191	5.01912	4.16838	2	18	00	0.24687	5.05416	4.24520
2	6	20	0.28089	5.02014	4.17062	2	18	20	0.24595	5.05508	4.24723
2	6	30	0.28037	5.02066	4.17173	2	18	30	0.24550	5.05553	4.24825
2	6	40	0.27986	5.02117	4.17285	2	18	40	0.24504	5.05599	4.24926
2	7	00	0.27884	5.02219	4.17507	2	19	00	0.24413	5.05690	4.25128
2	7	20	0.27782	5.02321	4.17729	2	19	20	0.24322	5.05781	4.25330
2	7	30	0.27731	5.02372	4.17839	2	19	30	0.24276	5.05827	4.25430
2	7	40	0.27680	5.02423	4.17950	2	19	40	0.24231	5.05872	4.25531
2	8	00	0.27579	5.02524	4.18171	2	20	00	0.24141	5.05962	4.25731
2	8	20	0.27478	5.02625	4.18391	2	20	20	0.24051	5.06052	4.25931
2	8	30	0.27428	5.02675	4.18500	2	20	30	0.24006	5.06097	4.26031
2	8	40	0.27378	5.02725	4.18610	2	20	40	0.23961	5.06142	4.26131
2	9	00	0.27277	5.02826	4.18828	2	21	00	0.23871	5.06232	4.26330
2	9	20	0.27177	5.02926	4.19047	2	21	20	0.23782	5.06321	4.26429
2	9	30	0.27127	5.02976	4.19156	2	21	30	0.23738	5.06365	4.26628
2	9	40	0.27077	5.03026	4.19265	2	21	40	0.23693	5.06410	4.26727
2	10	00	0.26978	5.03125	4.19482	2	22	00	0.23605	5.06498	4.26926
2	10	20	0.26879	5.03224	4.19698	2	22	20	0.23516	5.06587	4.27121
2	10	30	0.26830	5.03275	4.19806	2	22	30	0.23472	5.06631	4.27220
2	10	40	0.26781	5.03322	4.19914	2	22	40	0.23428	5.06675	4.27318
2	11	00	0.26682	5.03421	4.20129	2	23	00	0.23340	5.06763	4.27514
2	11	20	0.26584	5.03519	4.20344	2	23	20	0.23252	5.06851	4.27710
2	11	30	0.26535	5.03568	4.20451	2	23	30	0.23209	5.06894	4.27807
2	11	40	0.26486	5.03617	4.20558	2	23	40	0.23165	5.06938	4.27905
2	12	00	0.26389	5.03714	4.20771	2	24	00	0.23078	5.07025	4.28097

The New LOGARITHMIC SOLAR TABLES. 23

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising
2	24	20	0 22991	5.07112	4.28294	2	36	20	0.20035	5.10068	4.34980
2	24	30	0 22948	5.07155	4.28391	2	36	30	0.19996	5.10107	4 35069
2	24	40	0 22905	5.07198	4.28487	2	36	40	0 19957	5 10146	4 35158
2	25	00	0 22819	5.07284	4.28681	2	37	00	0.19880	5.10223	4 35335
2	25	20	0.22732	5.07371	4.28873	2	37	20	0 19803	5.10300	4 35512
2	25	30	0.22690	5 07413	4.28969	2	37	30	0.19764	5.10339	4.356 1
2	25	40	0 22647	5.07456	4.29065	2	37	40	0 19726	5 10377	4.35689
2	26	00	0.22561	5.07512	4.29257	2	38	00	0.19649	5 10454	4 35865
2	26	20	0.22476	5.07627	4.29449	2	38	20	0.19572	5.10531	4 36041
2	26	30	0.22433	5 07670	4.29544	2	38	30	0 19534	5.10569	4.36128
2	26	40	0 22391	5.07712	4.29639	2	38	40	0.19496	5.10607	4.36216
2	27	00	0.22306	5.07797.	4.29830	2	39	00	0 19420	5 10683	4 36391
2	27	20	0.22222	5.07881	4.30020	2	39	20	0.19344	5.10759	4 36565
2	27	30	0.22180	5.07923	4.30115	2	39	30	0.19306	5.10797	4 36653
2	27	40	0.22138	5.07965	4.30209	2	39	40	0.19269	5.10834	4.36740
2	28	00	0.22054	5.08049	4.30398	2	40	00	0.19193	5 10910	4 36913
2	28	20	0.21970	5 08133	4.30587	2	40	20	0 19118	5 10985	4 37087
2	28	30	0.21928	5 08175	4 30681	2	40	30	0.19081	5 11022	4 37173
2	28	40	0.21887	5.08216	4.30775	2	40	40	0.19043	5.11060	4.37260
2	29	00	0.21803	5.08300	4.30963	2	41	00	0.18968	5.11135	4 37432
2	29	20	0.21720	5.08383	4 31150	2	41	20	0.18894	5.11209	4.37604
2	29	30	0.21679	5.08424	4 31243	2	41	30	0.18857	5.11246	4 37690
2	29	40	0.21638	5 08465	4.31337	2	41	40	0.18820	5.11283	4.37776
2	30	00	0.21555	5.08548	4.31523	2	42	00	0.18746	5 11357	4.37948
2	30	20	0 21473	5.08630	4.31709	2	42	20	0 18672	5.11431	4.38119
2	30	30	0.21432	5 08671	4.31801	2	42	30	0 18635	5 11468	4 38204
2	30	40	0 21391	5.08712	4.31894	2	42	40	0.18598	5.11505	4 38289
2	31	00	0.21309	5.08794	4.32079	2	43	00	0 18525	5.11578	4.38459
2	31	20	0.21228	5.08875	4.32264	2	43	20	0.18451	5.11652	4 38629
2	31	30	0.21187	5.08916	4.32356	2	43	30	0.18415	5.11688	4.38714
2	31	40	0.21147	5.08956	4.32448	2	43	40	0.18378	5.11725	4.38799
2	32	00	0.21066	5.09037	4.32631	2	44	00	0.18306	5.11797	4.38968
2	32	20	0.20985	5.09118	4 32815	2	44	20	0.18233	5.11870	4.39137
2	32	30	0 20945	5.09158	4.32906	2	44	30	0 18197	5.11906	4 39221
2	32	40	0.20905	5 09198	4.32997	2	44	40	0.18161	5.11942	4.39305
2	33	00	0.20824	5 09279	4.33180	2	45	00	0.18089	5.12014	4.39473
2	33	20	0.20744	5.09359	4.33362	2	45	20	0.18017	5.12086	4.39641
2	33	30	0.20704	5.09399	4.33453	2	45	30	0.17981	5.12122	4.39725
2	33	40	0.20665	5.09438	4 33543	2	45	40	0 17945	5.12158	4.39808
2	34	00	0 20585	5.09518	4.33724	2	46	00	0.17874	5.12229	4.39975
2	34	20	0.20506	5 09597	4.33905	2	46	20	0.17802	5.12301	4 30142
2	34	30	0 20466	5.09637	4.33995	2	46	30	0.17767	5 12336	4.30225
2	34	40	0.20427	5.09676	4.34085	2	46	40	0.17731	5.12372	4.40308
2	35	00	0.20348	5.09755	4.34265	2	47	00	0.17660	5.12443	4.40474
2	35	20	0.20269	5.09834	4.34444	2	47	20	0.17590	5.12513	4.40639
2	35	30	0.20230	5.09873	4.34534	2	47	30	0.17554	5.12549	4 40722
2	35	40	0 20191	5.09912	4.34623	2	47	40	0.17519	5.12584	4.40804
2	36	00	0.20113	5.09990	4.34802	2	48	00	0.17449	5.12654	4.40969

24 The New LOGARITHMIC SOLAR TABLES.

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
2	48	20	0.17379	5.12724	4.41133	3	00	20	0.14988	5.15115	4.46823
2	48	30	0.17344	5.12759	4.41215	3	00	30	0.14957	5.15146	4.46899
2	48	40	0.17309	5.12794	4.41297	3	00	40	0.14926	5.15177	4.46975
2	49	00	0.17239	5.12864	4.41461	3	01	00	0.14863	5.15240	4.47127
2	49	20	0.17170	5.12933	4.41624	3	1	20	0.14800	5.15303	4.47278
2	49	30	0.17135	5.12968	4.41706	3	1	30	0.14769	5.15334	4.47354
2	49	40	0.17101	5.13002	4.41787	3	1	40	0.14738	5.15365	4.47430
2	50	00	0.17032	5.13071	4.41950	3	2	00	0.14676	5.15427	4.47580
2	50	20	0.16963	5.13140	4.42112	3	2	20	0.14614	5.15489	4.47731
2	50	30	0.16928	5.13175	4.42193	3	2	30	0.14583	5.15520	4.47806
2	50	40	0.16894	5.13209	4.42274	3	2	40	0.14552	5.15551	4.47881
2	51	00	0.16826	5.13277	4.42435	3	3	00	0.14490	5.15613	4.48031
2	51	20	0.16758	5.13345	4.42597	3	3	20	0.14429	5.15674	4.48180
2	51	30	0.16724	5.13379	4.42677	3	3	30	0.14398	5.15705	4.48255
2	51	40	0.16690	5.13413	4.42758	3	3	40	0.14368	5.15735	4.48330
2	52	00	0.16622	5.13481	4.42918	3	4	00	0.14307	5.15796	4.48479
2	52	20	0.16554	5.13549	4.43078	3	4	20	0.14246	5.15857	4.48627
2	52	30	0.16520	5.13583	4.43158	3	4	30	0.14215	5.15888	4.48701
2	52	40	0.16487	5.13616	4.43238	3	4	40	0.14185	5.15918	4.48776
2	53	00	0.16419	5.13684	4.43398	3	5	00	0.14124	5.15979	4.48924
2	53	20	0.16352	5.13751	4.43557	3	5	20	0.14064	5.16039	4.49071
2	53	30	0.16319	5.13784	4.43636	3	5	30	0.14034	5.16069	4.49145
2	53	40	0.16285	5.13818	4.43716	3	5	40	0.14004	5.16099	4.49219
2	54	00	0.16219	5.13884	4.43874	3	6	00	0.13944	5.16159	4.49365
2	54	20	0.16152	5.13951	4.44032	3	6	20	0.13884	5.16219	4.49513
2	54	30	0.16119	5.13984	4.44111	3	6	30	0.13854	5.16249	4.49586
2	54	40	0.16086	5.14017	4.44190	3	6	40	0.13824	5.16279	4.49659
2	55	00	0.16020	5.14083	4.44348	3	7	00	0.13765	5.16338	4.49806
2	55	20	0.15954	5.14149	4.44505	3	7	20	0.13705	5.16398	4.49952
2	55	30	0.15921	5.14182	4.44583	3	7	30	0.13676	5.16427	4.40024
2	55	40	0.15888	5.14215	4.44662	3	7	40	0.13646	5.16457	4.50098
2	56	00	0.15823	5.14280	4.44818	3	8	00	0.13587	5.16516	4.50243
2	56	20	0.15758	5.14345	4.44974	3	8	20	0.13528	5.16575	4.50388
2	56	30	0.15725	5.14378	4.45052	3	8	30	0.13499	5.16604	4.50461
2	56	40	0.15692	5.14411	4.45130	3	8	40	0.13470	5.16633	4.50533
2	57	00	0.15628	5.14475	4.45286	3	9	00	0.13411	5.16692	4.50677
2	57	20	0.15563	5.14540	4.45441	3	9	20	0.13353	5.16750	4.50822
2	57	30	0.15530	5.14573	4.45518	3	9	30	0.13324	5.16779	4.50894
2	57	40	0.15498	5.14605	4.45596	3	9	40	0.13295	5.16808	4.50966
2	58	00	0.15434	5.14669	4.45750	3	10	00	0.13237	5.16866	4.51109
2	58	20	0.15370	5.14733	4.45904	3	10	20	0.13179	5.16924	4.51253
2	58	30	0.15338	5.14765	4.45981	3	10	30	0.13150	5.16953	4.51325
2	58	40	0.15306	5.14797	4.46058	3	10	40	0.13121	5.16982	4.51396
2	59	00	0.15242	5.14861	4.46212	3	11	00	0.13064	5.17039	4.51539
2	59	20	0.15178	5.14925	4.46365	3	11	20	0.13007	5.17096	4.51681
2	59	30	0.15146	5.14957	4.46442	3	11	30	0.12978	5.17125	4.51753
2	59	40	0.15115	5.14988	4.46518	3	11	40	0.12950	5.17153	4.51824
3	00	00	0.15051	5.15052	4.46671	3	12	00	0.12893	5.17210	4.51966

The New LOGARITHMIC SOLAR TABLES. 25

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
3	12	20	0.12836	5.17267	4.52107	3	24	20	0.10899	5.19204	4.57032
3	12	30	0.12807	5.17296	4.52178	3	24	30	0.10873	5.19230	4.57098
3	12	40	0.12779	5.17324	4.52249	3	24	40	0.10848	5.19255	4.57164
3	13	00	0.12723	5.17380	4.52390	3	25	00	0.10797	5.19306	4.57296
3	13	20	0.12666	5.17437	4.52531	3	25	20	0.10746	5.19357	4.57428
3	13	30	0.12638	5.17465	4.52601	3	25	30	0.10721	5.19382	4.57494
3	13	40	0.12610	5.17493	4.52672	3	25	40	0.10696	5.19407	4.57559
3	14	00	0.12554	5.17549	4.52812	3	26	00	0.10646	5.19457	4.57690
3	14	20	0.12499	5.17604	4.52952	3	26	20	0.10595	5.19508	4.57821
3	14	30	0.12471	5.17632	4.53022	3	26	30	0.10570	5.19533	4.57886
3	14	40	0.12443	5.17660	4.53092	3	26	40	0.10545	5.19558	4.57951
3	15	00	0.12387	5.17716	4.53231	3	27	00	0.10495	5.19608	4.58082
3	15	20	0.12332	5.17771	4.53371	3	27	20	0.10446	5.19657	4.58212
3	15	30	0.12305	5.17798	4.53440	3	27	30	0.10421	5.19682	4.58277
3	15	40	0.12277	5.17826	4.43510	3	27	40	0.10396	5.19707	4.58342
3	16	00	0.12222	5.17881	4.53648	3	28	00	0.10347	5.19756	4.58471
3	16	20	0.12167	5.17936	4.53787	3	28	20	0.10297	5.19806	4.58601
3	16	30	0.12140	5.17963	4.53856	3	28	30	0.10272	5.19831	4.58665
3	16	40	0.12113	5.17990	4.53925	3	28	40	0.10248	5.19855	4.58730
3	17	00	0.12058	5.18045	4.54063	3	29	00	0.10199	5.19904	4.58859
3	17	20	0.12004	5.18099	4.54201	3	29	20	0.10151	5.19952	4.58988
3	17	30	0.11977	5.18126	4.54269	3	29	30	0.10126	5.19977	4.59052
3	17	40	0.11949	5.18154	4.54338	3	29	40	0.10102	5.20001	4.59116
3	18	00	0.11895	5.18208	4.54475	3	30	00	0.10053	5.20050	4.59244
3	18	20	0.11842	5.18261	4.54612	3	30	20	0.10005	5.20098	4.59372
3	18	30	0.11815	5.18288	4.54680	3	30	30	0.09981	5.20122	4.59436
3	18	40	0.11788	5.18315	4.54749	3	30	40	0.09957	5.20146	4.59500
3	19	00	0.11734	5.18369	4.54885	3	31	00	0.09909	5.20194	4.59627
3	19	20	0.11681	5.18422	4.55021	3	31	20	0.09861	5.20242	4.59755
3	19	30	0.11654	5.18449	4.55089	3	31	30	0.09837	5.20266	4.59818
3	19	40	0.11628	5.18475	4.55157	3	31	40	0.09813	5.20290	4.59882
3	20	00	0.11575	5.18528	4.55293	3	32	00	0.09765	5.20338	4.60008
3	20	20	0.11522	5.18581	4.55428	3	32	20	0.09718	5.20385	4.60135
3	20	30	0.11495	5.18608	4.55496	3	32	30	0.09694	5.20409	4.60198
3	20	40	0.11469	5.18634	4.55563	3	32	40	0.09670	5.20433	4.60261
3	21	00	0.11416	5.18687	4.55698	3	33	00	0.09623	5.20480	4.60387
3	21	20	0.11364	5.18739	4.55832	3	33	20	0.09576	5.20527	4.60513
3	21	30	0.11338	5.18765	4.55900	3	33	30	0.09552	5.20551	4.60576
3	21	40	0.11312	5.18791	4.55967	3	33	40	0.09529	5.20574	4.60639
3	22	00	0.11259	5.18844	4.56101	3	34	00	0.09482	5.20621	4.60764
3	22	20	0.11207	5.18896	4.56235	3	34	20	0.09435	5.20668	4.60890
3	22	30	0.11181	5.18922	4.56301	3	34	30	0.09412	5.20691	4.60952
3	22	40	0.11155	5.18948	4.56368	3	34	40	0.09389	5.20714	4.61015
3	23	00	0.11104	5.18999	4.56501	3	35	00	0.09343	5.20760	4.61139
3	23	20	0.11052	5.19051	4.56634	3	35	20	0.09296	5.20807	4.61264
3	23	30	0.11027	5.19076	4.56701	3	35	30	0.09273	5.20830	4.61326
3	23	40	0.11001	5.19102	4.56767	3	35	40	0.09250	5.20853	4.61388
3	24	00	0.10950	5.19153	4.56900	3	36	00	0.09204	5.20899	4.61512

26 The New LOGARITHMIC SOLAR TABLES.

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
3	36	20	0.09158	5.20945	4.61636	3	48	20	0.07000	5.22503	4.65952
3	36	30	0.09136	5.20967	4.61698	3	48	30	0.07579	5.22524	4.66010
3	36	40	0.09113	5.20990	4.61760	3	48	40	0.07559	5.22544	4.66068
3	37	00	0.09067	5.21036	4.61883	3	49	00	0.07518	5.22585	4.66184
3	37	20	0.09022	5.21081	4.62006	3	49	20	0.07478	5.22625	4.66299
3	37	30	0.08999	5.21104	4.62068	3	49	30	0.07458	5.22645	4.66357
3	37	40	0.08976	5.21127	4.62129	3	49	40	0.07437	5.22666	4.66415
3	38	00	0.08931	5.21172	4.62252	3	50	00	0.07397	5.22706	4.66530
3	38	20	0.08886	5.21217	4.62375	3	50	20	0.07357	5.22746	4.66645
3	38	30	0.08864	5.21239	4.62436	3	50	30	0.07337	5.22766	4.66702
3	38	40	0.08842	5.21261	4.62497	3	50	40	0.07317	5.22786	4.66760
3	39	00	0.08797	5.21306	4.62619	3	51	00	0.07277	5.22826	4.66874
3	39	20	0.08752	5.21351	4.62741	3	51	20	0.07237	5.22866	4.66989
3	39	30	0.08730	5.21373	4.62802	3	51	30	0.07217	5.22886	4.67046
3	39	40	0.08708	5.21395	4.62863	3	51	40	0.07197	5.22906	4.67103
3	40	00	0.08664	5.21439	4.62984	3	52	00	0.07158	5.22945	4.67217
3	40	20	0.08619	5.21484	4.63105	3	52	20	0.07119	5.22984	4.67331
3	40	30	0.08597	5.21506	4.63166	3	52	30	0.07099	5.23004	4.67388
3	40	40	0.08575	5.21528	4.63226	3	52	40	0.07079	5.23024	4.67445
3	41	00	0.08531	5.21572	4.63347	3	53	00	0.07040	5.23063	4.67558
3	41	20	0.08488	5.21615	4.63468	3	53	20	0.07001	5.23102	4.67671
3	41	30	0.08466	5.21637	4.63528	3	53	30	0.06982	5.23121	4.67728
3	41	40	0.08444	5.21659	4.63588	3	53	40	0.06962	5.23141	4.67785
3	42	00	0.08401	5.21702	4.63708	3	54	00	0.06923	5.23180	4.67897
3	42	20	0.08357	5.21746	4.63828	3	54	20	0.06885	5.23218	4.68010
3	42	30	0.08336	5.21767	4.63888	3	54	30	0.06865	5.23238	4.68066
3	42	40	0.08314	5.21789	4.63948	3	54	40	0.06845	5.23257	4.68123
3	43	00	0.08271	5.21832	4.64068	3	55	00	0.06808	5.23295	4.68235
3	43	20	0.08228	5.21875	4.64187	3	55	20	0.06770	5.23333	4.68347
3	43	30	0.08207	5.21896	4.64246	3	55	30	0.06751	5.23352	4.68403
3	43	40	0.08185	5.21918	4.64306	3	55	40	0.06731	5.23372	4.68459
3	44	00	0.08143	5.21960	4.64425	3	56	00	0.06693	5.23410	4.68517
3	44	20	0.08100	5.22003	4.64544	3	56	20	0.06655	5.23447	4.68682
3	44	30	0.08079	5.22024	4.64603	3	56	30	0.06637	5.23466	4.68738
3	44	40	0.08058	5.22045	4.64662	3	56	40	0.06618	5.23485	4.68794
3	45	00	0.08015	5.22088	4.64780	3	57	00	0.06580	5.23523	4.68905
3	45	20	0.07973	5.22130	4.64898	3	57	20	0.06543	5.23560	4.69016
3	45	30	0.07952	5.22151	4.64957	3	57	30	0.06524	5.23579	4.69071
3	45	40	0.07931	5.22172	4.65016	3	57	40	0.06505	5.23598	4.69127
3	46	00	0.07889	5.22214	4.65134	3	58	00	0.06468	5.23635	4.69237
3	46	20	0.07848	5.22255	4.65251	3	58	20	0.06431	5.23672	4.69348
3	46	30	0.07827	5.22276	4.65310	3	58	30	0.06412	5.23691	4.69403
3	46	40	0.07806	5.22297	4.65369	3	58	40	0.06394	5.23709	4.69458
3	47	00	0.07765	5.22338	4.65486	3	59	00	0.06357	5.23746	4.69568
3	47	20	0.07723	5.22380	4.65602	3	59	20	0.06320	5.23783	4.69678
3	47	30	0.07703	5.22400	4.65661	3	59	30	0.06302	5.23801	4.69733
3	47	40	0.07682	5.22421	4.65719	3	59	40	0.06283	5.23820	4.69787
3	48	00	0.07641	5.22462	4.65836	4	00	00	0.06247	5.23856	4.69897

The New LOGARITHMIC SOLAR TABLES. 27

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
4	0	20	0.06211	5.23892	4.70006	4	12	20	0.04980	5.25123	4.73823
4	0	30	0.06192	5.23911	4.70061	4	12	30	0.04964	5.25139	4.73874
4	0	40	0.06174	5.23929	4.70115	4	12	40	0.04948	5.25155	4.73926
4	1	00	0.06138	5.23965	4.70224	4	13	00	0.04916	5.25187	4.74028
4	1	20	0.06102	5.24001	4.70333	4	13	20	0.04884	5.25219	4.74131
4	1	30	0.06084	5.24019	4.70387	4	13	30	0.04868	5.25235	4.74182
4	1	40	0.06066	5.24037	4.70442	4	13	40	0.04852	5.25251	4.74233
4	2	00	0.06030	5.24073	4.70550	4	14	00	0.04821	5.25282	4.74335
4	2	20	0.05995	5.24108	4.70658	4	14	20	0.04789	5.25314	4.74437
4	2	30	0.05977	5.24126	4.70712	4	14	30	0.04774	5.25329	4.74488
4	2	40	0.05959	5.24144	4.70766	4	14	40	0.04758	5.25345	4.74539
4	3	00	0.05924	5.24179	4.70874	4	15	00	0.04727	5.25376	4.74641
4	3	20	0.05888	5.24215	4.70928	4	15	20	0.04696	5.25407	4.74742
4	3	30	0.05871	5.24232	4.71036	4	15	30	0.04680	5.25423	4.74793
4	3	40	0.05853	5.24250	4.71089	4	15	40	0.04665	5.25438	4.74844
4	4	00	0.05818	5.24285	4.71197	4	16	00	0.04634	5.25469	4.74945
4	4	20	0.05783	5.24320	4.71304	4	16	20	0.04603	5.25500	4.75046
4	4	30	0.05766	5.24337	4.71357	4	16	30	0.04588	5.25515	4.75096
4	4	40	0.05748	5.24355	4.71411	4	16	40	0.04573	5.25530	4.75147
4	5	00	0.05714	5.24389	4.71518	4	17	00	0.04542	5.25561	4.75247
4	5	20	0.05679	5.24424	4.71624	4	17	20	0.04512	5.25591	4.75348
4	5	30	0.05662	5.24441	4.71678	4	17	30	0.04496	5.25607	4.75398
4	5	40	0.05645	5.24458	4.71731	4	17	40	0.04481	5.25622	4.75448
4	6	00	0.05610	5.24493	4.71837	4	18	00	0.04451	5.25652	4.75549
4	6	20	0.05576	5.24527	4.71943	4	18	20	0.04421	5.25682	4.75649
4	6	30	0.05559	5.24544	4.71996	4	18	30	0.04406	5.25697	4.75699
4	6	40	0.05542	5.24561	4.72049	4	18	40	0.04391	5.25712	4.75748
4	7	00	0.05508	5.24595	4.72155	4	19	00	0.04361	5.25742	4.75848
4	7	20	0.05474	5.24629	4.72260	4	19	20	0.04332	5.25771	4.75948
4	7	30	0.05457	5.24646	4.72313	4	19	30	0.04317	5.25786	4.75997
4	7	40	0.05440	5.24663	4.72366	4	19	40	0.04302	5.25801	4.76047
4	8	00	0.05406	5.24697	4.72471	4	20	00	0.04272	5.25831	4.76146
4	8	20	0.05373	5.24730	4.72576	4	20	20	0.04243	5.25860	4.76245
4	8	30	0.05356	5.24747	4.72628	4	20	30	0.04228	5.25875	4.76295
4	8	40	0.05340	5.24763	4.72681	4	20	40	0.04214	5.25889	4.76344
4	9	00	0.05306	5.24797	4.72785	4	21	00	0.04185	5.25918	4.76443
4	9	20	0.05273	5.24830	4.72890	4	21	20	0.04155	5.25948	4.76542
4	9	30	0.05257	5.24846	4.72942	4	21	30	0.04141	5.25962	4.76591
4	9	40	0.05240	5.24863	4.72994	4	21	40	0.04127	5.25976	4.76640
4	10	00	0.05207	5.24896	4.73098	4	22	00	0.04098	5.26005	4.76738
4	10	20	0.05174	5.24929	4.73202	4	22	20	0.04069	5.26034	4.76836
4	10	30	0.05158	5.24945	4.73254	4	22	30	0.04055	5.26048	4.76885
4	10	40	0.05142	5.24961	4.73306	4	22	40	0.04040	5.26063	4.76934
4	11	00	0.05109	5.24994	4.73410	4	23	00	0.04012	5.26091	4.77032
4	11	20	0.05076	5.25027	4.73514	4	23	20	0.03983	5.26120	4.77130
4	11	30	0.05060	5.25043	4.73565	4	23	30	0.03969	5.26134	4.77179
4	11	40	0.05044	5.25059	4.73617	4	23	40	0.03955	5.26148	4.77227
4	12	00	0.05012	5.25091	4.73720	4	24	00	0.03927	5.26176	4.77325

28 The New LOGARITHMIC SOLAR TABLES.

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
4	24	20	0.03899	5.26204	4.77422	4	36	20	0.02961	5.27142	4.80820
4	24	30	0.03885	5.26218	4.77470	4	36	30	0.02949	5.27154	4.80866
4	24	40	0.03871	5.26232	4.77519	4	36	40	0.02937	5.27166	4.80912
4	25	00	0.03843	5.26260	4.77616	4	37	00	0.02913	5.27190	4.8104
4	25	10	0.03815	5.26288	4.77713	4	37	10	0.02889	5.27214	4.81095
4	25	20	0.03802	5.26301	4.77761	4	37	20	0.02877	5.27226	4.81141
4	25	30	0.03788	5.26315	4.77809	4	37	30	0.02865	5.27238	4.81186
4	26	00	0.03760	5.26343	4.77906	4	38	00	0.02841	5.27262	4.81277
4	26	10	0.03733	5.26370	4.78002	4	38	10	0.02818	5.27285	4.81368
4	26	20	0.03719	5.26384	4.78050	4	38	20	0.02806	5.27297	4.81414
4	26	30	0.03706	5.26397	4.78098	4	38	30	0.02794	5.27309	4.81459
4	26	40	0.03678	5.26425	4.78194	4	39	00	0.02771	5.27332	4.81550
4	27	00	0.03651	5.26452	4.78290	4	39	10	0.02748	5.27355	4.81641
4	27	10	0.03638	5.26465	4.78338	4	39	20	0.02736	5.27367	4.81686
4	27	20	0.03624	5.26479	4.78385	4	39	30	0.02724	5.27379	4.81731
4	28	00	0.03597	5.26506	4.78481	4	40	00	0.02701	5.27402	4.81821
4	28	10	0.03571	5.26532	4.78576	4	40	10	0.02678	5.27425	4.81911
4	28	20	0.03557	5.26546	4.78624	4	40	20	0.02667	5.27436	4.81956
4	28	30	0.03544	5.26559	4.78671	4	40	30	0.02656	5.27447	4.82001
4	29	00	0.03517	5.26586	4.78767	4	41	00	0.02633	5.27470	4.82091
4	29	10	0.03491	5.26612	4.78861	4	41	10	0.02610	5.27493	4.82181
4	29	20	0.03478	5.26625	4.78908	4	41	20	0.02599	5.27504	4.82226
4	29	30	0.03465	5.26638	4.78956	4	41	30	0.02588	5.27515	4.82271
4	29	40	0.03438	5.26665	4.79051	4	41	40	0.02565	5.27538	4.82360
4	30	00	0.03412	5.26691	4.79145	4	42	00	0.02543	5.27560	4.82449
4	30	10	0.03399	5.26704	4.79192	4	42	10	0.02532	5.27571	4.82494
4	30	20	0.03386	5.26717	4.79240	4	42	20	0.02521	5.27582	4.82538
4	31	00	0.03360	5.26743	4.79334	4	43	00	0.02499	5.27604	4.82628
4	31	10	0.03335	5.26768	4.79428	4	43	10	0.02477	5.27626	4.82716
4	31	20	0.03322	5.26781	4.79475	4	43	20	0.02466	5.27637	4.82761
4	31	30	0.03309	5.26794	4.79522	4	43	30	0.02455	5.27648	4.82805
4	32	00	0.03283	5.26820	4.79615	4	44	00	0.02433	5.27670	4.82894
4	32	10	0.03258	5.26845	4.79709	4	44	10	0.02411	5.27692	4.82982
4	32	20	0.03245	5.26858	4.79756	4	44	20	0.02400	5.27703	4.83026
4	32	30	0.03233	5.26870	4.79802	4	44	30	0.02390	5.27713	4.83071
4	32	40	0.03207	5.26896	4.79896	4	44	40	0.02368	5.27735	4.83159
4	33	00	0.03182	5.26921	4.79989	4	45	00	0.02347	5.27756	4.83247
4	33	10	0.03170	5.26933	4.80035	4	45	10	0.02336	5.27767	4.83291
4	33	20	0.03157	5.26946	4.80082	4	45	20	0.02326	5.27777	4.83335
4	34	00	0.03132	5.26971	4.80175	4	46	00	0.02304	5.27799	4.83423
4	34	10	0.03107	5.26996	4.80267	4	46	10	0.02283	5.27800	4.83510
4	34	20	0.03095	5.27008	4.80314	4	46	20	0.02273	5.27830	4.83554
4	34	30	0.03083	5.27020	4.80360	4	46	30	0.02262	5.27841	4.83598
4	35	00	0.03058	5.27045	4.80452	4	47	00	0.02241	5.27862	4.83685
4	35	10	0.03034	5.27069	4.80544	4	47	10	0.02221	5.27882	4.83773
4	35	20	0.03021	5.27082	4.80591	4	47	20	0.02210	5.27893	4.83816
4	35	30	0.03009	5.27094	4.80637	4	47	30	0.02200	5.27903	4.83860
4	35	40	0.02984	5.27118	4.80729	4	47	40	0.02179	5.27924	4.83947
4	36	00				4	48	00			

The New LOGARITHMIC SOLAR TABLES.

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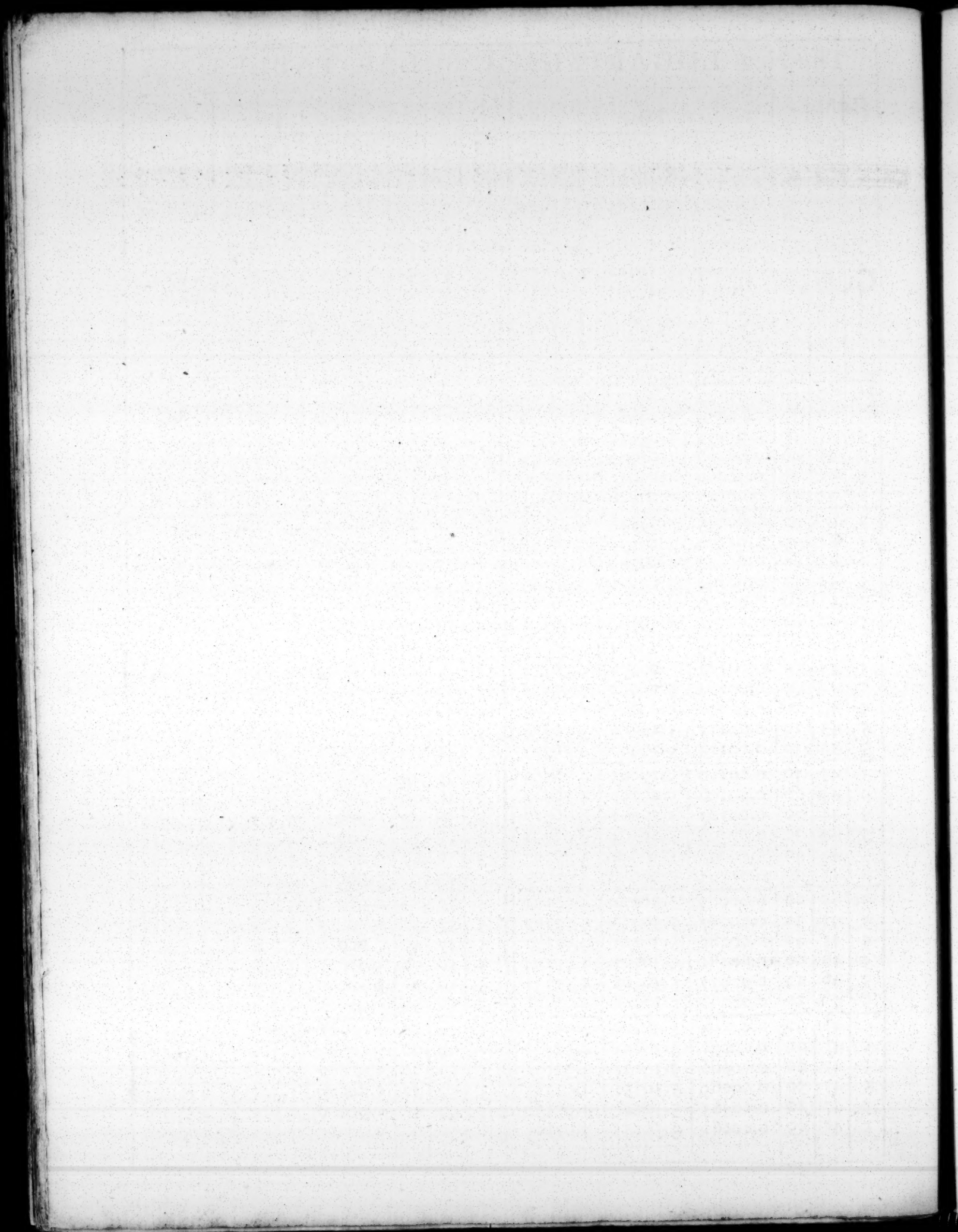
H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
4	48	20	0.02159	5.27944	4.84034	5	0	20	0.01489	5.28614	4.87075
4	48	30	0.02149	5.27954	4.84077	5	0	30	0.01480	5.28623	4.87116
4	48	40	0.02139	5.27964	4.84120	5	0	40	0.01472	5.28631	4.87157
4	49	00	0.02128	5.27985	4.84207	5	1	00	0.01455	5.28648	4.87239
4	49	20	0.02098	5.28005	4.84293	5	1	20	0.01439	5.28664	4.87321
4	49	30	0.02088	5.28015	4.84337	5	1	30	0.01430	5.28673	4.87362
4	49	40	0.02078	5.28025	4.84380	5	1	40	0.01422	5.28681	4.87402
4	50	00	0.02058	5.28045	4.84466	5	2	00	0.01406	5.28697	4.87484
4	50	20	0.02038	5.28065	4.84552	5	2	20	0.01390	5.28713	4.87566
4	50	30	0.02028	5.28075	4.84595	5	2	30	0.01381	5.28722	4.87606
4	50	40	0.02018	5.28085	4.84638	5	2	40	0.01373	5.28730	4.87647
4	51	00	0.01999	5.28104	4.84724	5	3	00	0.01357	5.28746	4.87728
4	51	20	0.01979	5.28124	4.84810	5	3	20	0.01341	5.28762	4.87809
4	51	30	0.01969	5.28134	4.84852	5	3	30	0.01333	5.28770	4.87850
4	51	40	0.01960	5.28143	4.84895	5	3	40	0.01325	5.28778	4.87890
4	52	00	0.01940	5.28163	4.84981	5	4	00	0.01310	5.28793	4.87971
4	52	20	0.01921	5.28182	4.85066	5	4	20	0.01294	5.28809	4.88052
4	52	30	0.01912	5.28191	4.85108	5	4	30	0.01286	5.28817	4.88093
4	52	40	0.01902	5.28201	4.85151	5	4	40	0.01278	5.28825	4.88133
4	53	00	0.01883	5.28220	4.85236	5	5	00	0.01263	5.28840	4.88213
4	53	20	0.01864	5.28239	4.85321	5	5	20	0.01247	5.28856	4.88294
4	53	30	0.01854	5.28249	4.85363	5	5	30	0.01240	5.28863	4.88334
4	53	40	0.01845	5.28258	4.85406	5	5	40	0.01232	5.28871	4.88374
4	54	00	0.01826	5.28277	4.85490	5	6	00	0.01217	5.28886	4.88454
4	54	20	0.01808	5.28295	4.85575	5	6	20	0.01202	5.28901	4.88534
4	54	30	0.01798	5.28305	4.85617	5	6	30	0.01194	5.28909	4.88574
4	54	40	0.01789	5.28314	4.85659	5	6	40	0.01187	5.28916	4.88614
4	55	00	0.01771	5.28332	4.85744	5	7	00	0.01172	5.28931	4.88694
4	55	20	0.01752	5.28351	4.85828	5	7	20	0.01157	5.28946	4.88774
4	55	30	0.01743	5.28360	4.85870	5	7	30	0.01150	5.28953	4.88814
4	55	40	0.01734	5.28369	4.85912	5	7	40	0.01142	5.28961	4.88853
4	56	00	0.01716	5.28387	4.85996	5	8	00	0.01128	5.28975	4.88933
4	56	20	0.01698	5.28405	4.86079	5	8	20	0.01113	5.28990	4.89012
4	56	30	0.01689	5.28414	4.86121	5	8	30	0.01106	5.28997	4.89052
4	56	40	0.01680	5.28423	4.86163	5	8	40	0.01099	5.29004	4.89091
4	57	00	0.01662	5.28441	4.86246	5	9	00	0.01084	5.29019	4.89171
4	57	20	0.01644	5.28459	4.86330	5	9	20	0.01070	5.29033	4.89250
4	57	30	0.01635	5.28468	4.86372	5	9	30	0.01063	5.29040	4.89289
4	57	40	0.01626	5.28477	4.86413	5	9	40	0.01056	5.29047	4.89328
4	58	00	0.01609	5.28494	4.86496	5	10	00	0.01042	5.29061	4.89407
4	58	20	0.01591	5.28512	4.86579	5	10	20	0.01028	5.29075	4.89486
4	58	30	0.01583	5.28520	4.86621	5	10	30	0.01021	5.29082	4.89525
4	58	40	0.01574	5.28529	4.86662	5	10	40	0.01014	5.29089	4.89564
4	59	00	0.01557	5.28546	4.86745	5	11	00	0.01000	5.29101	4.89643
4	59	20	0.01540	5.28563	4.86828	5	11	20	0.00987	5.29116	4.89721
4	59	30	0.01531	5.28572	4.86869	5	11	30	0.00980	5.29123	4.89760
4	59	40	0.01523	5.28580	4.86910	5	11	40	0.00973	5.29130	4.89799
5	00	00	0.01506	5.28597	4.86992	5	12	00	0.00960	5.29143	4.89877

30 The New LOGARITHMIC SOLAR TABLES.

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
5	12	20	0.00946	5.28157	4.89955	5	24	20	0.00528	5.29575	4.92686
5	12	30	0.00940	5.28163	4.89994	5	24	30	0.00523	5.29580	4.92723
5	12	40	0.00933	5.28170	4.90033	5	24	40	0.00518	5.29585	4.92760
5	13	00	0.00920	5.28183	4.90111	5	25	00	0.00508	5.29595	4.92833
5	13	20	0.00907	5.29190	4.90188	5	25	20	0.00499	5.29604	4.92907
5	13	30	0.00900	5.29203	4.90227	5	25	30	0.00494	5.29609	4.92944
5	13	40	0.00894	5.29209	4.90266	5	25	40	0.00489	5.29614	4.92980
5	14	00	0.00881	5.29222	4.90345	5	26	00	0.00480	5.29623	4.93054
5	14	20	0.00868	5.29235	4.90421	5	26	20	0.00470	5.29633	4.93127
5	14	30	0.00862	5.29241	4.90459	5	26	30	0.00466	5.29637	4.93164
5	14	40	0.00855	5.29248	4.90498	5	26	40	0.00461	5.29642	4.93200
5	15	00	0.00843	5.29260	4.90575	5	27	00	0.00452	5.29651	4.93273
5	15	20	0.00830	5.29273	4.90652	5	27	20	0.00443	5.29660	4.93340
5	15	30	0.00824	5.29279	4.90690	5	27	30	0.00438	5.29665	4.93383
5	15	40	0.00818	5.29285	4.90728	5	27	40	0.00434	5.29669	4.93419
5	16	00	0.00805	5.29298	4.90805	5	28	00	0.00425	5.29678	4.93492
5	16	20	0.00793	5.29310	4.90882	5	28	20	0.00416	5.29687	4.93564
5	16	30	0.00787	5.29316	4.90920	5	28	30	0.00412	5.29691	4.93600
5	16	40	0.00781	5.29322	4.90958	5	28	40	0.00407	5.29696	4.93637
5	17	00	0.00769	5.29334	4.91034	5	29	00	0.00399	5.29704	4.93709
5	17	20	0.00757	5.29346	4.91111	5	29	20	0.00390	5.29713	4.93781
5	17	30	0.00751	5.29352	4.91149	5	29	30	0.00386	5.29717	4.93817
5	17	40	0.00745	5.29358	4.91187	5	29	40	0.00382	5.29721	4.93854
5	18	00	0.00733	5.29370	4.91263	5	30	00	0.00373	5.29730	4.93926
5	18	20	0.00722	5.29381	4.91339	5	30	20	0.00365	5.29738	4.93998
5	18	30	0.00716	5.29387	4.91377	5	30	30	0.00361	5.29742	4.94034
5	18	40	0.00710	5.29393	4.91415	5	30	40	0.00357	5.29746	4.94069
5	19	00	0.00699	5.29404	4.91490	5	31	00	0.00349	5.29754	4.94141
5	19	20	0.00687	5.29416	4.91566	5	31	20	0.00341	5.29762	4.94213
5	19	30	0.00682	5.29421	4.91603	5	31	30	0.00337	5.29766	4.94249
5	19	40	0.00676	5.29427	4.91641	5	31	40	0.00333	5.29770	4.94284
5	20	00	0.00665	5.29438	4.91716	5	32	00	0.00325	5.29778	4.94356
5	20	20	0.00654	5.29449	4.91792	5	32	20	0.00317	5.29786	4.94427
5	20	30	0.00648	5.29455	4.91830	5	32	30	0.00313	5.29790	4.94463
5	20	40	0.00643	5.29460	4.91867	5	32	40	0.00310	5.29793	4.94498
5	21	00	0.00632	5.29471	4.91942	5	33	00	0.00302	5.29801	4.94570
5	21	20	0.00621	5.29482	4.92017	5	33	20	0.00295	5.29808	4.94641
5	21	30	0.00616	5.29487	4.92054	5	33	30	0.00291	5.29812	4.94676
5	21	40	0.00610	5.29493	4.92092	5	33	40	0.00287	5.29816	4.94712
5	22	00	0.00600	5.29503	4.92166	5	34	00	0.00280	5.29823	4.94782
5	22	20	0.00589	5.29514	4.92241	5	34	20	0.00273	5.29830	4.94853
5	22	30	0.00584	5.29519	4.92278	5	34	30	0.00269	5.29834	4.94888
5	22	40	0.00579	5.29524	4.92315	5	34	40	0.00266	5.29837	4.94924
5	23	00	0.00568	5.29535	4.92390	5	35	00	0.00259	5.29844	4.94994
5	23	20	0.00558	5.29545	4.92464	5	35	20	0.00252	5.29851	4.95065
5	23	30	0.00553	5.29550	4.92501	5	35	30	0.00249	5.29854	4.95100
5	23	40	0.00548	5.29555	4.92538	5	35	40	0.00245	5.29858	4.95135
5	24	00	0.00538	5.29565	4.92612	5	36	00	0.00239	5.29864	4.95205

The New LOGARITHMIC SOLAR TABLES. 31

H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.	H	M	S	$\frac{1}{2}$ Elapsed Time.	Middle Time.	Rising.
5	36	20	0.00232	5.29871	4.95275	5	48	20	0.00056	5.30047	4.97732
5	36	30	0.00229	5.29874	4.95310	5	48	30	0.00055	5.30048	4.97765
5	36	40	0.00225	5.29878	4.95345	5	48	40	0.00053	5.30050	4.97798
5	37	00	0.00219	5.29884	4.95415	5	49	00	0.00050	5.30053	4.97865
5	37	20	0.00213	5.29890	4.95485	5	49	20	0.00047	5.30056	4.97931
5	37	30	0.00210	5.29893	4.95520	5	49	30	0.00046	5.30057	4.97964
5	37	40	0.00207	5.29896	4.95555	5	49	40	0.00044	5.30059	4.97997
5	38	00	0.00200	5.29903	4.95624	5	50	00	0.00041	5.30062	4.98063
5	38	20	0.00194	5.29909	4.95694	5	50	20	0.00039	5.30064	4.98129
5	38	30	0.00191	5.29912	4.95728	5	50	30	0.00037	5.30066	4.98162
5	38	40	0.00188	5.29915	4.95763	5	50	40	0.00036	5.30067	4.98195
5	39	00	0.00183	5.29920	4.95832	5	51	00	0.00033	5.30070	4.98261
5	39	20	0.00177	5.29926	4.95902	5	51	20	0.00031	5.30072	4.98326
5	39	30	0.00174	5.29929	4.95936	5	51	30	0.00030	5.30073	4.98359
5	39	40	0.00171	5.29932	4.95971	5	51	40	0.00029	5.30074	4.98392
5	40	00	0.00166	5.29937	4.96040	5	52	00	0.00026	5.30077	4.98457
5	40	20	0.00160	5.29943	4.96109	5	52	20	0.00024	5.30079	4.98523
5	40	30	0.00157	5.29946	4.96143	5	52	30	0.00023	5.30080	4.98555
5	40	40	0.00155	5.29948	4.96177	5	52	40	0.00022	5.30081	4.98588
5	41	00	0.00149	5.29954	4.96246	5	53	00	0.00020	5.30083	4.98653
5	41	20	0.00144	5.29959	4.96315	5	53	20	0.00018	5.30085	4.98718
5	41	30	0.00142	5.29961	4.96349	5	53	30	0.00017	5.30086	4.98751
5	41	40	0.00139	5.29964	4.96383	5	53	40	0.00017	5.30086	4.98783
5	42	00	0.00134	5.29969	4.96451	5	54	00	0.00015	5.30083	4.98848
5	42	20	0.00129	5.29974	4.96520	5	54	20	0.00013	5.30090	4.98913
5	42	30	0.00127	5.29976	4.96554	5	54	30	0.00013	5.30090	4.98945
5	42	40	0.00124	5.29979	4.96588	5	54	40	0.00012	5.30091	4.98978
5	43	00	0.00120	5.29983	4.96656	5	55	00	0.00010	5.30093	4.99042
5	43	20	0.00115	5.29988	4.96724	5	55	20	0.00009	5.30094	4.99107
5	43	30	0.00113	5.29990	4.96758	5	55	30	0.00008	5.30095	4.99139
5	43	40	0.00110	5.29993	4.96792	5	55	40	0.00008	5.30095	4.99171
5	44	00	0.00106	5.29997	4.96860	5	56	00	0.00007	5.30096	4.99235
5	44	20	0.00102	5.30001	4.96927	5	56	20	0.00006	5.30097	4.99300
5	44	30	0.00099	5.30004	4.96961	5	56	30	0.00005	5.30098	4.99332
5	44	40	0.00097	5.30006	4.96995	5	56	40	0.00005	5.30098	4.99364
5	45	00	0.00093	5.30010	4.97062	5	57	00	0.00004	5.30099	4.99428
5	45	20	0.00089	5.30014	4.97130	5	57	20	0.00003	5.30100	4.99492
5	45	30	0.00087	5.30016	4.97163	5	57	30	0.00003	5.30100	4.99524
5	45	40	0.00085	5.30018	4.97197	5	57	40	0.00002	5.30101	4.99556
5	46	00	0.00081	5.30022	4.97264	5	58	00	0.00002	5.30101	4.99619
5	46	20	0.00077	5.30026	4.97331	5	58	20	0.00001	5.30102	4.99683
5	46	30	0.00075	5.30028	4.97365	5	58	30	0.00001	5.30102	4.99715
5	46	40	0.00074	5.30029	4.97398	5	58	40	0.00001	5.30102	4.99747
5	47	00	0.00070	5.30033	4.97465	5	59	00	0.00000	5.30102	4.99810
5	47	20	0.00066	5.30037	4.97532	5	59	20	0.00000	5.30103	4.99873
5	47	30	0.00065	5.30038	4.97565	5	59	30	0.00000	5.30103	4.99905
5	47	40	0.00063	5.30040	4.97599	5	59	40	0.00000	5.30103	4.99937
5	48	00	0.00060	5.30043	4.97665	6	00	00	0.00000	5.30103	5.00000



General CONSTRUCTION of the foregoing LOGARITHMIC TABLES.

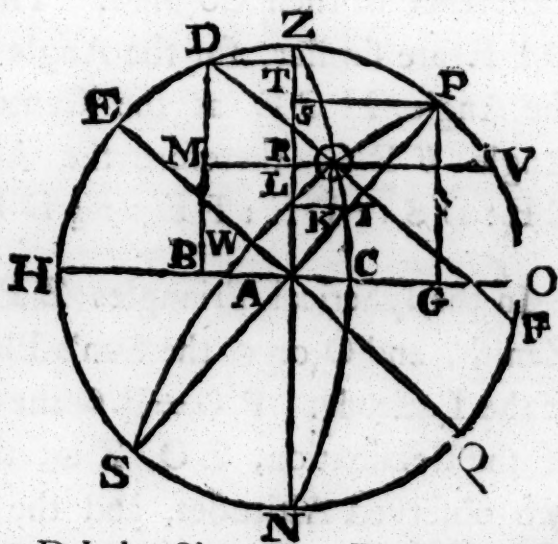
IN Order to facilitate the Method of calculating the Numbers in these Tables, it may be necessary to premise the two subsequent Lemmas :

L E M M A I.

The Rectangle of the Sines (to the Radius 1) of any two Sides of a spherical Triangle, drawn into the Co-sine of the Angle they include, being added to the Rectangle of their Co-sines, will be equal to the Co-sine of the third Side.

D E M O N S T R A T I O N.

Let $H Z O N$ represent the Plane of a Section of a Sphere passing through its Center A , upon which imagine two great Circles thereof, as $Z \odot N$, $P \odot S$, orthographically projected, \odot their Point of Intersection; draw the Diameters $Z N$, $P S$, and at right Angles to the latter draw $Q A E$, to which draw $F \odot D$ parallel: This done, let $O A H$ be drawn perpendicular to $Z N$, and let fall the Perpendiculars $P G$, $P S$, $D B$, $D T$, $V \odot M$, $I L$, and $\odot K$; then in the spherical Triangle $Z P \odot$, $A W$ will represent the Co-sine (Radius being $A E$) of the Angle $Z P \odot$, $D I$ the Sine of $\odot P$ ($D P$) $A I$ its Co-sine, $P S$ the Sine of $Z P$, $A S$ its Co-sine. Now $A E : A W :: D I \odot I$ (by the Property of the Ellipse) also by similar Triangles $A E : P G ::$



K

A I

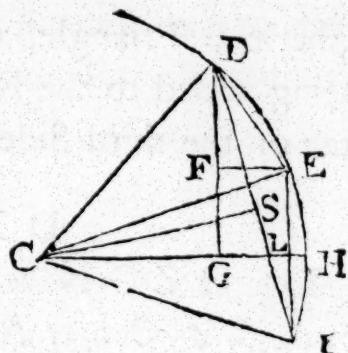
$AI:AL$ and $AE:AG::\odot I:\odot K=RL$ therefore $AR=AL+RL=\frac{AI \times PG}{AE} + \frac{DI \times AW}{AE} \times \frac{AG}{AE}$; which (making $AE=1$) becomes $AI \times PG + DI \times AW \times AG$. Q.E.D.

LEMMA II.

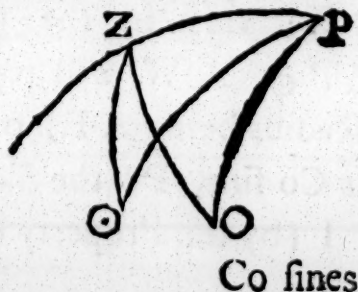
As Radius is to the Sine of half the Sum of any two Arches or Angles, so is the Sine of half their Difference to half the Difference of the Co sines of the same two Arches.

DEMONSTRATION.

Let DH and HI be two given Arches; make $HE=HI$, then will ED be the Difference of those Arches, draw the Radii CD, CE, CH and CI , also the Chords IE, ED and DI , let fall CS and DG Perpendiculars to ID and CH respectively; lastly, draw EF parallel to CH , then will DS be the Sine of half the Sum of the proposed Arches, DE twice the Sine of half their Difference, and $EF (=GL)$ the Difference of their Co-sines. The Triangles, CDS, DFE are similar, for the Angle IDE at the Circumference is equal to the Angle HCE at the Center, equal, because of Parallels, to the Angle FEC , therefore the Angle $CDS = \text{Angle } DEF$; whence $CE:DS::DE:FE::\frac{1}{2}DE:\frac{1}{2}EF$. Q.E.D.



In the spherical Triangles $ZPO, ZP\odot$, let P be the Pole, Z the Zenith, and O or \odot the Sun's Place; then will PZ be the Complement of the Latitude. $PO=P\odot$ the the Sun's Polar Distance or Complement of the Declination, $ZO, Z\odot$, the Complement of two observed Altitudes, and the Angle $OP\odot$ the Difference of Time between those Observations.



Put m for the Rectangle of the natural Sines (Radius 1) of ZP and $P\odot$, n for that of their

Co-sines, a and b for the Sines of the observed Altitude, or the Co-sines of $Z O$, and $Z \odot$ respectively; x for the Co-sine of the Angle $Z P \odot$, y for the Co-sine of $Z P O$, and for the Sine of half the Angle $O P \odot$, put s . Then by Lemma I. $m x + n = b$, and $m y + n = a$, hence, by Subtraction, $m x - y = b - a$. By Lemma II. we have $1 : \text{Sine } \frac{1}{2} Z P \odot + \frac{1}{2} Z P O :: \text{Sine of } \frac{1}{2} O P \odot : \frac{1}{2} \text{ the Difference of the Co-sines of the Angles } Z P \odot, Z P O$; that is $1 : \text{Sine } \frac{1}{2} Z P \odot + \frac{1}{2} Z P O :: s : \frac{x-y}{2}$

but from the Equation above we have $\frac{x-y}{2} = \frac{b-a}{2m}$, hence, by Substitu-

tion $\frac{b-a}{2ms} = \text{Sine } \frac{1}{2} Z P \odot + \frac{1}{2} Z P O$, or the Sine of $Z P \odot + \frac{1}{2} O P \odot$,

which in Words at length, gives this general Rule. Take the natural Sine of the observed Altitudes, and subtract the less from the greater, noting their Difference. Then take the natural Co-sines of the Latitude and Declination, and twice the natural Sine of half the Difference of Time, (converted into Degrees and Minutes; between the Observations; multiply these three Quantities together, by which Product divide the reserved Difference, and the Quotient will give the natural Sine of an Angle, (which must be reduced to equatorial Time) corresponding to the mean, or middle Time, so called in the Tables, because it is half the Sum of the two Hour Angles from Noon.

In order to shew the Practice of this Rule, let the first Example at page 12, be again proposed, where there is given the Sun's Declination, $11^{\circ} 17'$ North, and at 10h. 2m. in the Forenoon the Sun's Altitude was $46^{\circ} 55m$. then again at 11h. 27m. the second Altitude was $54^{\circ} 7'$. Latitude by Account is $46^{\circ} 50'$ North, required the true Latitude, and true Time of the Day, when the greatest Altitude was taken?

S O L U T I O N.

The natural Sine of Alt. $54^{\circ} 7'$ ————— .810212

The natural Sine of Alt. $46^{\circ} 55'$ ————— .730361

—————
Difference .079851

The natural Co-sine of Lat. $46^{\circ} 50'$ ————— .684122

The natural Co-sine of Declination $11^{\circ} 17'$ ————— .980672

The Time of Observation, 11h. 27m. and 10h. 2m. their Difference 1h. 25m. its half oh. 42m. 30s. to which answers $10^{\circ} 37\frac{1}{2}$ twice the natural Sine thereof is .36876, therefore multiply .68412, .98067 and .36876, together, their Product becomes .2474, by which dividing the reserved Difference .079851, the quotient .32276 is the natural Sine of $18^{\circ} 49\frac{1}{2}$, which converted into Time, allowing 15° to an Hour, as usual, gives 1h. 15m. and 18s. very near, for the mean or middle Time required, From which subtract 42m. 30s. half the elapsed Time, and there will remain 32m. 48s. the true Time from Noon, when the greatest Altitude was taken.

From a due Consideration of the above general Rule and its Example, it will not be difficult to point out the Method of constructing these Tables; for expounding the said Rule in Logarithms, we have Log.

$$b - a + \text{Log} \frac{1}{m} + \text{Log} \frac{1}{2} + \text{Log} \frac{1}{s} = \text{Log. Sine of Middle Time, or}$$

putting R for the former Part, $R + \text{Log} \frac{1}{s} = \text{Log. M. T.}$ Now, as

R remains constantly the same, it will, by applying this Theorem to the Construction of the Tables, evidently appear that the Columns marked *Half Elapsed Time*, contain the Arith. Comp. of the Sines of half the elapsed Time, equalled to Degrees and Minutes, thus against two Hours we find 3.30103 the Arith. Comp. of the Log. of the Sine of 30° , and against three Hours we have 0.15051, which is the Arith. Comp. of the Sine of 45° .

In this Manner the other Numbers in those Columns are determined.

By resuming the original Equation, viz. $\frac{b-a}{2ms} = \text{Sine MT}$, we

have $\text{Log. } b-a + \text{Log. } \frac{1}{m} + \text{Log. } \frac{1}{2s} = \text{Log. Sine MT}$, and there-

fore as $\text{Log. } b-a + \text{Log. } \frac{1}{m}$ may be considered as unaffected by s , it

follows that the Numbers in the Column marked *Middle Time*, are the respective Logarithms of twice s , that is of twice the natural Sines of the Times in Degrees, which they stand against, or which is the same Thing, the Logarithms of the Chords of double those Times reduced into Degrees, as before. Thus against three Hours we find 5.15052, which is the Logarithm of twice the natural Sine of 45° , against four Hours stands 5.23856, the Logarithm of twice the natural Sine of 60° , and the like for any other.

It only now remains to shew the Construction of the Numbers in the last Column, marked *Rising*, to do this take again the general Equation $\frac{b-a}{2ms} = \text{the Sine of ZP} \odot + \odot \text{PO}$, which, when the Sun is upon

the Meridian, will become $\frac{b-a}{2ms} = s$, wherein b now represents the Sine

of the Sun's Meridian Altitude) and consequently $\frac{b-a}{m} = 2s^2$, which

shews that the Numbers in the Column marked *Rising*, are proportional to $2s^2$. And because by the Property of the Circle, the Square of the Chord is equal to the Rectangle under the Diameter and versed Sine, it follows that the Numbers in the said Column are the Logarithmic versed Sines of the Times reduced to Degrees, against which they stand; Radius being Unity as before.

Note,

Note, In these Tables the Logarithmic Radix is supposed to be 100000 and consequently the greatest Index 5, which regulates the inferior Indices, and likewise shews that the natural Sines and versed Sines, can at most consist of but five Places of Figures: And moreover that the Sum of each corresponding Pair of Numbers in the Columns of *Half Elapsed* and *Middle Time* constantly make 5.30103, answering to the Logarithm of 200000 the double Radix.



F I N I S.

50 - 3474

30.30 2506

11.30 960
60
696

50
60
3000

960

3000

72.7

2.9030

3.4771

10.4913

7.4072

2.0380

2247 3.3516

749

ABRACADABRA
ABRACADABR
ABRACADAB
ABRACADA
ABRACAD
ABRACA
ABRAC
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ABR
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Monday
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Monday

Monday	17	N 14 W	93	81	42	26.57	53.17	0.47	2362
Tuesday	18	N 27 W	93	81	42	26.57	53.17	0.47	2362
Wednesday	19	N 63 W	130	60	116	25.57	55.26	2.9	2380
Thursday	20	N 74 W	119	32	114	25.25	57.32	2.0	2502
Friday	21	N 79 W	114	21	112	25.4	59.30	2.6	2614
Saturday	22	N 80 W	140	4	140	25.0	62.21	2.43	2762
Sunday	23	N 86 W	116	0	116	25.0	64.29	2.8	2870
Monday	24	N 102 W	47	6	42	25.14	65.15	0.46	2920
Tuesday	25	N 108 W	135	4	136	25.10	67.45	2.30	3056
Wednesday	26	N 105 W	145	12	144	25.30	70.24	2.39	3200
Thursday	27	N 119 W	62	39	20	26.29	70.46	0.22	3220
Friday	28	N 71 W	34	34	4	25.55	70.51	0.5	3224
Saturday	29	N 80 E	20	3	20	25.52	70.29	0.22	3202
Sunday	30	N 72 W	55	17	52	25.35	71.27	0.58	3254
Monday	1	N 34 W	19	11	15	25.46	71.46	0.16	3269
Tuesday	2	N 81 W	19	3	19	25.43	72.4	0.21	3280
Wednesday	3	N 84 W	36	4	36	25.47	72.44	0.40	3324
Thursday	4	N 40 W	45	30	33	26.17	73.21	0.37	3357
Friday	5	N 37 W	115	92	69	27.49	74.39	1.10	3426
Saturday	6	N 32 W	156	96	123	29.25	76.57	2.10	3549
Sunday	7	N 100 W	25	18	31	31.18	78.26		

CT N 69 W 363 L.

CT N 53.01 W 210 L.

ES. N 46 W. 137 L.

CT N 51 W 02 L.
Lat P 06.31.18. Lat. V. 0.00
145. 30.33